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Fondo europeo di sviluppo regionale



Regione Emilia-Romagna

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# Planetary gear modelling/optimization; Experiments on coated gears

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# Planetary gear modelling/ optimization

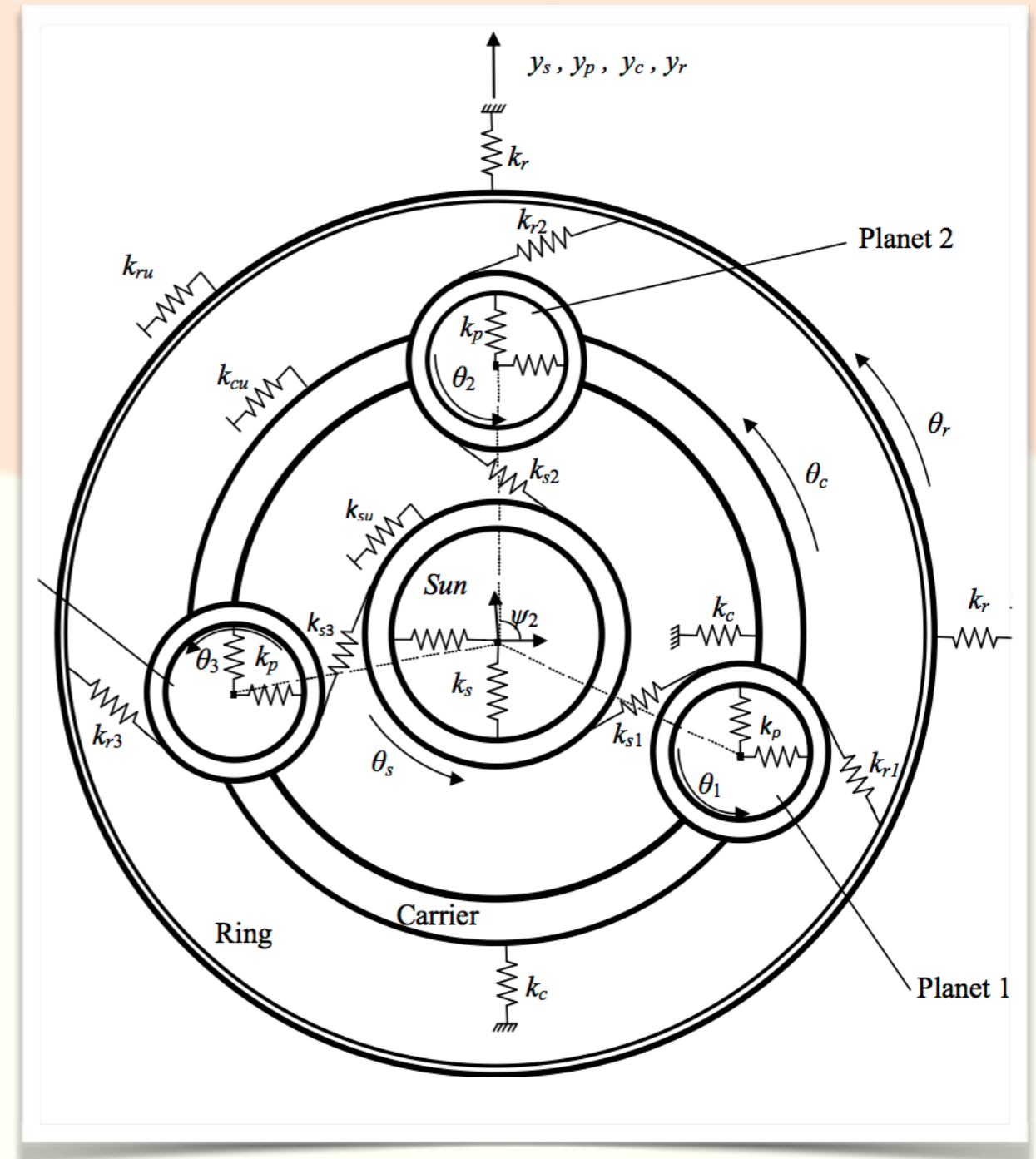


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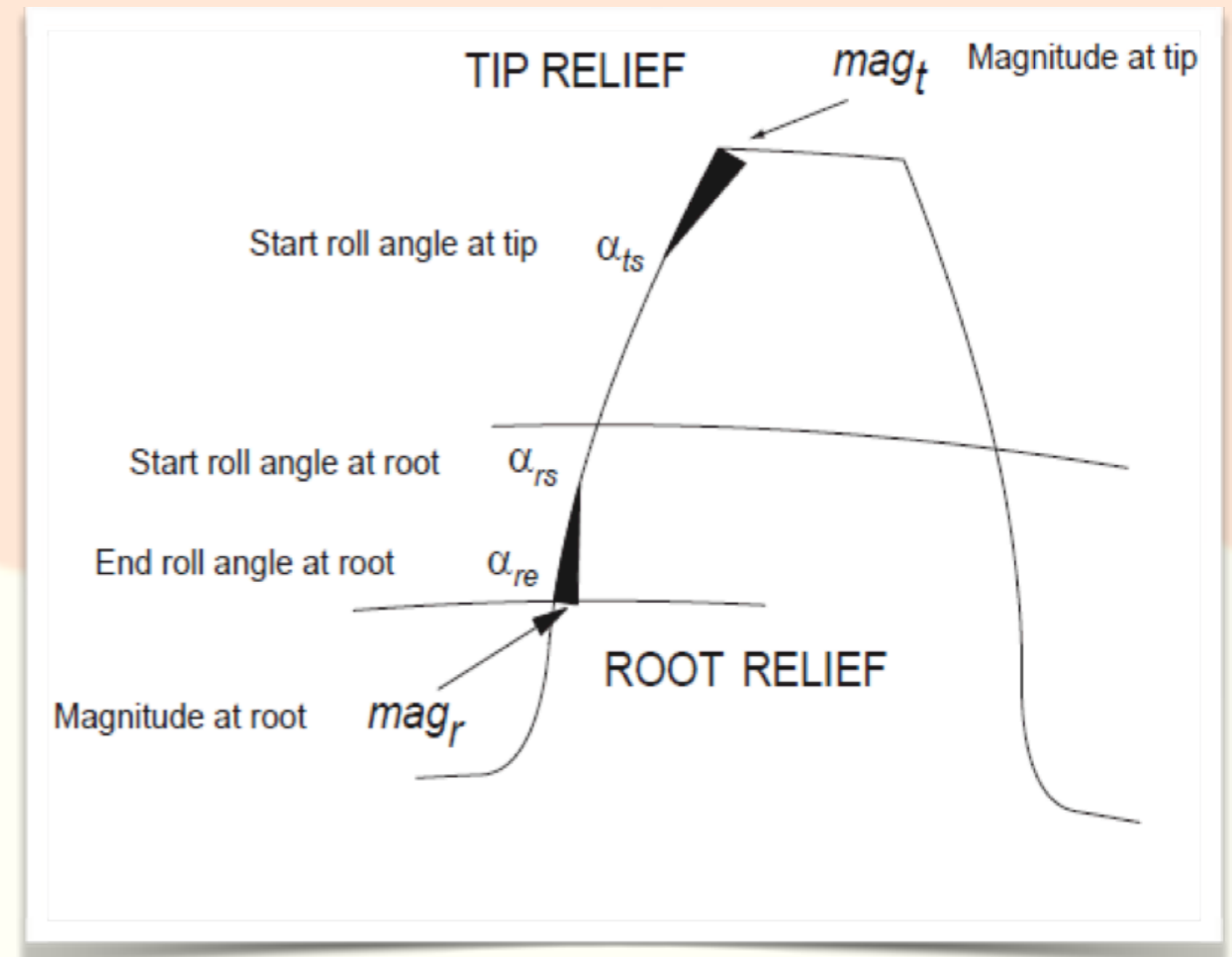
# Planetary gear modelling

- ❖ The goal was to find optimal profile modifications in order to reduce the overall vibration (Gear day 2017)
- ❖ Dynamic behavior of planetary gear can be modeled using lumped parameter model
- ❖ Tip and root relief on sun and planets are considered (no modifications on the ring)
- ❖ The model includes:
  - ❖ FE evaluated stiffnesses of gear pairs
  - ❖ Backlash in the contacts
  - ❖ Geometric errors due top profile modifications
  - ❖ Bearing stiffness



# Optimization of profile reliefs

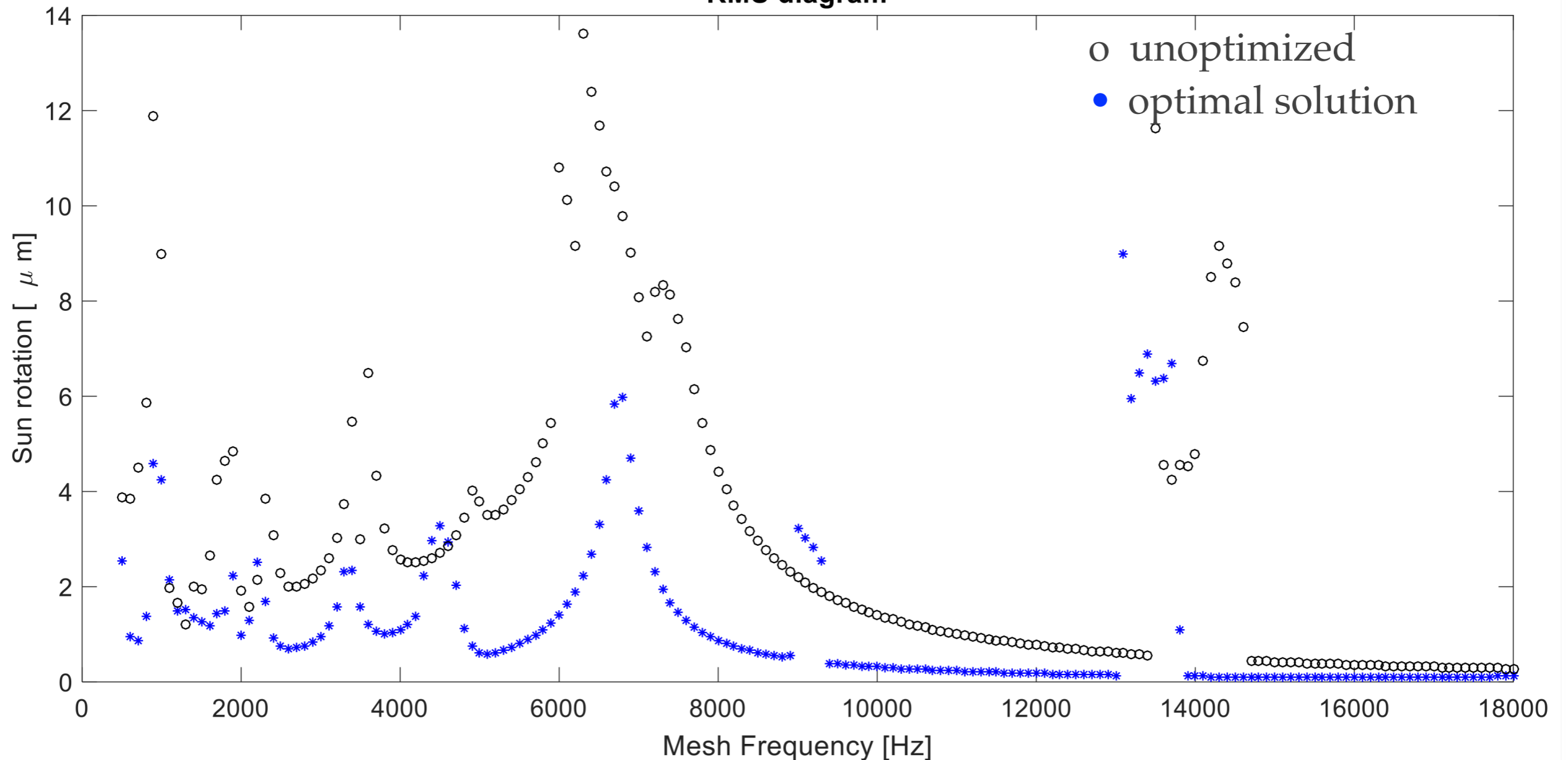
- ❖ Optimization parameters:
  - ❖ Sun profile reliefs (tip and root)
  - ❖ Planet profile reliefs (tip and root)
- ❖ Objective function:
  - ❖ Peak to peak of the STE of the planetary gear
- ❖ No modifications on ring



Pinion				Gear			
$\alpha_{ts}$	$mag_t$	$\alpha_{rs}$	$mag_r$	$\alpha_{ts}$	$mag_t$	$\alpha_{rs}$	$mag_r$
11 bits	6 bits	11 bits	6 bits	11 bits	6 bits	11 bits	6 bits
0110...	01..						...01

# Planetary gear optimisation

RMS diagram



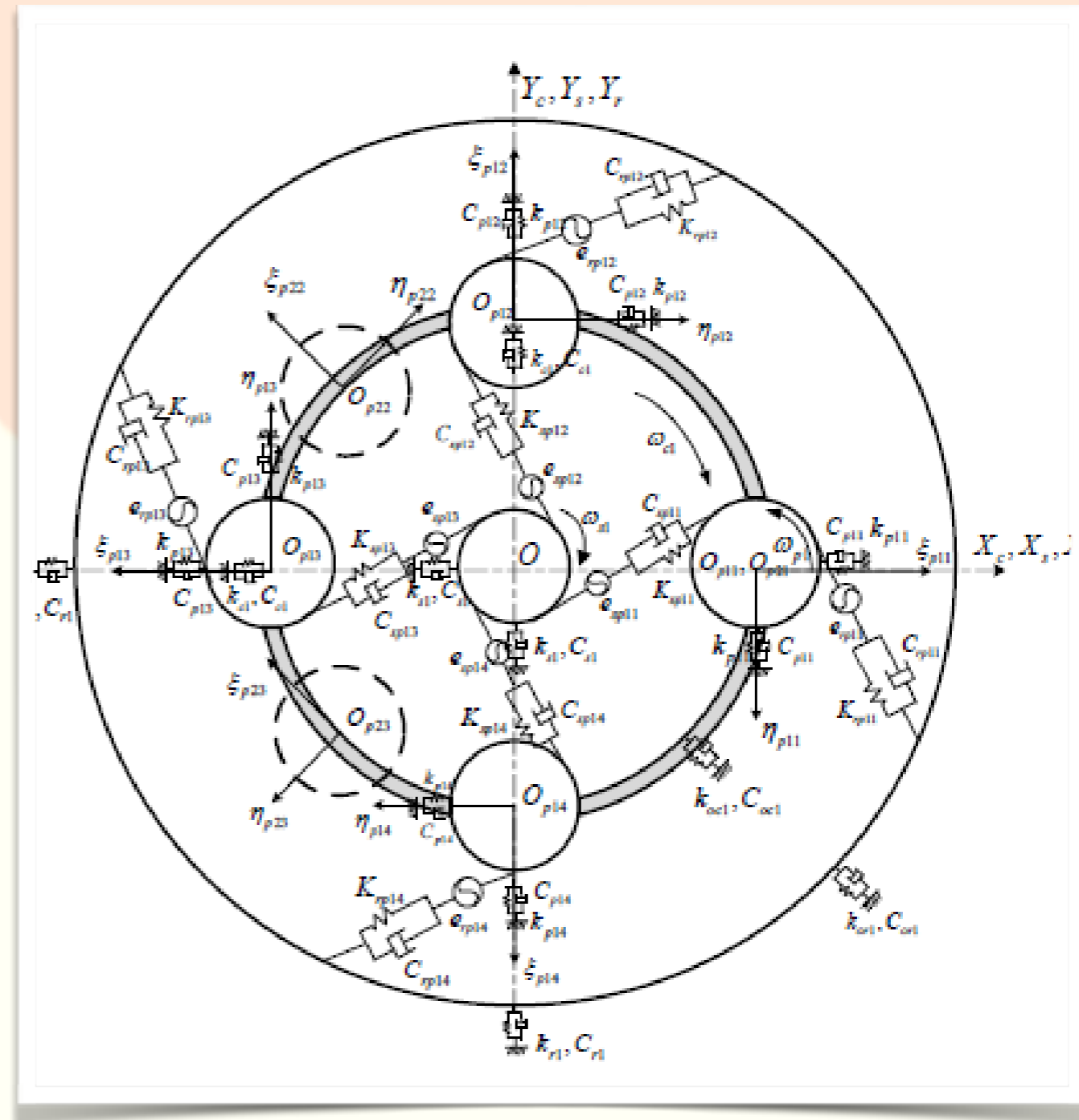
- ❖ Optimization (Genetic Algorithms) of the overall Static Transmission Error STE allows for reducing the Dynamic Transmission Error DTE at each mesh frequency

# Evaluating Load Sharing Coefficient

- ❖ In a system having four or more planets, static load imbalance occurs
- ❖ Load sharing coefficient is a measure of the average force on the  $i$ -th planet

$$L_i = \frac{\frac{1}{T_m} \int_0^{T_m} F_i(t) dt}{M_1 / R_1}$$

- ❖ The dynamic model can be adapted in order to evaluate the load sharing coefficient



# Evaluating Load Sharing Coefficient

## Numerical analysis

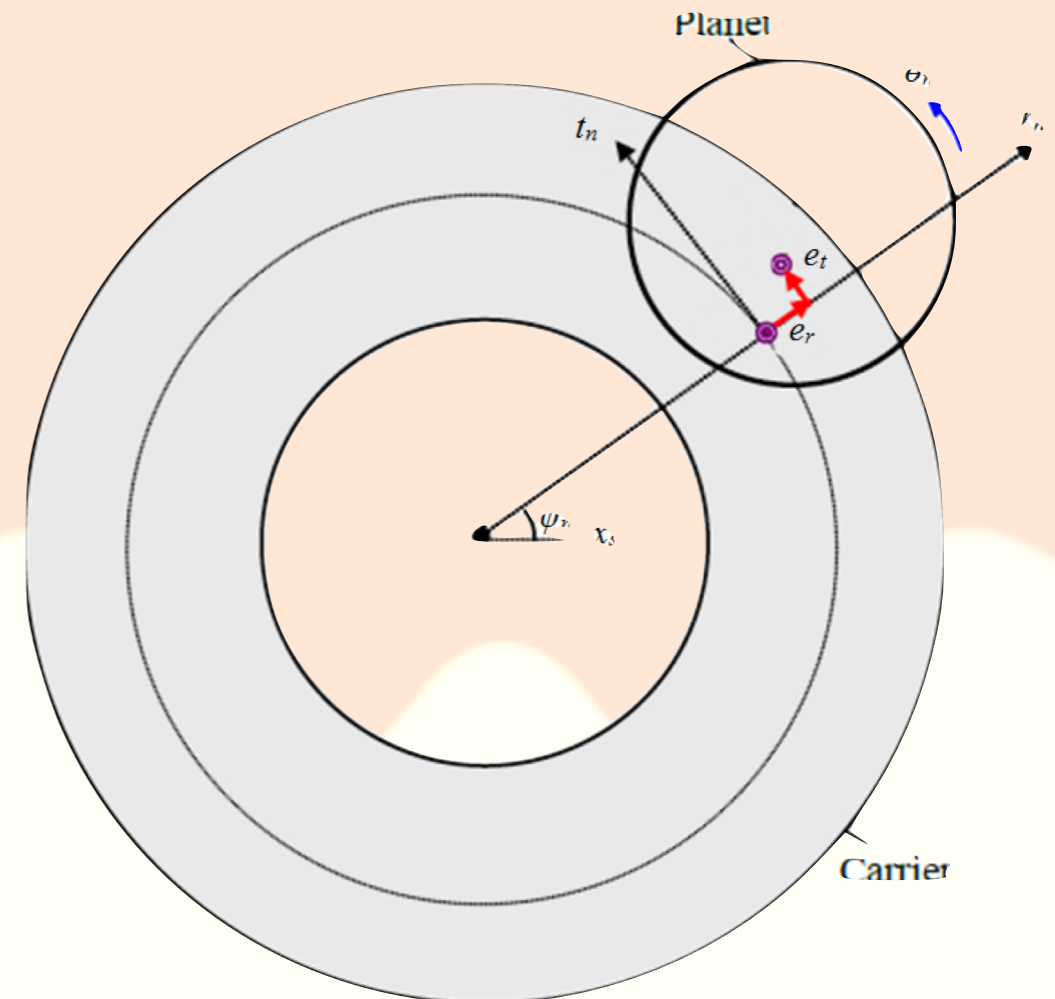
- ❖ Dynamic load-sharing sensitivity to errors which could provide references for designing planetary gears and load balancing.

The main sources of imbalance are:

- ❖ Carrier pinhole position error (the most significant)
- ❖ Planet size variation
- ❖ Run-out errors of the gears

## Case study:

- ❖ 2D spur planetary gearbox with N equally spaced planets
- ❖ Nonlinear model with time varying mesh stiffnesses and backlash
- ❖ 200 micron positioning error of 2nd planet in tangential direction



# Evaluating Load Sharing Coefficient

Angular position of the n-th planet

$$\hat{\psi}_n = \psi_n + a \tan\left(\frac{e_t}{e_r + cd}\right) \quad \psi_n + \frac{e_t}{e_r + cd}$$

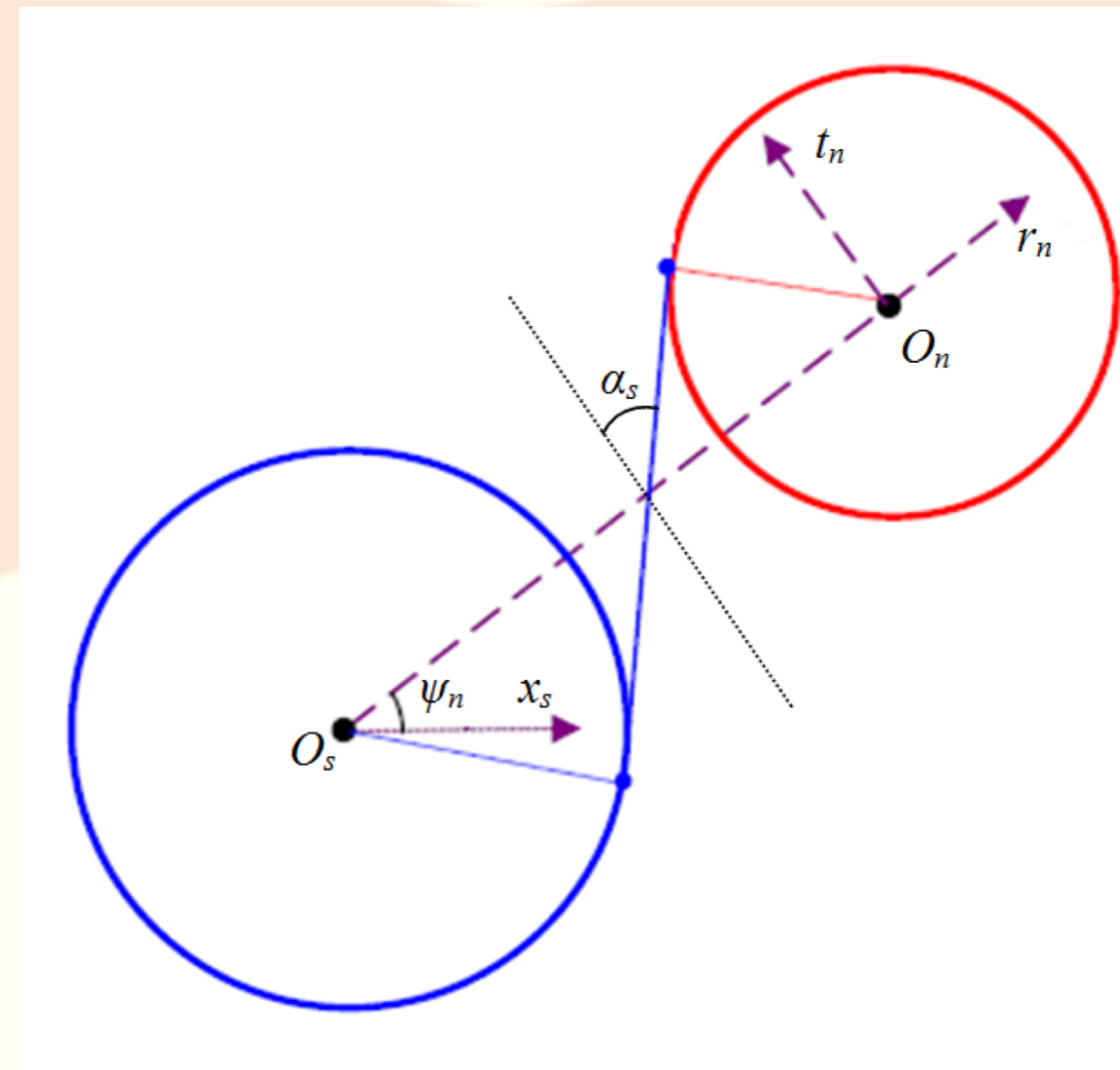
Center distance

$$cd = \sqrt{(cd + e_r)^2 + e_t^2}$$

Pressure angle

$$\hat{\alpha}_{s/r} = a \cos\left(\frac{r_{bs} \pm r_{bn}}{cd}\right)$$

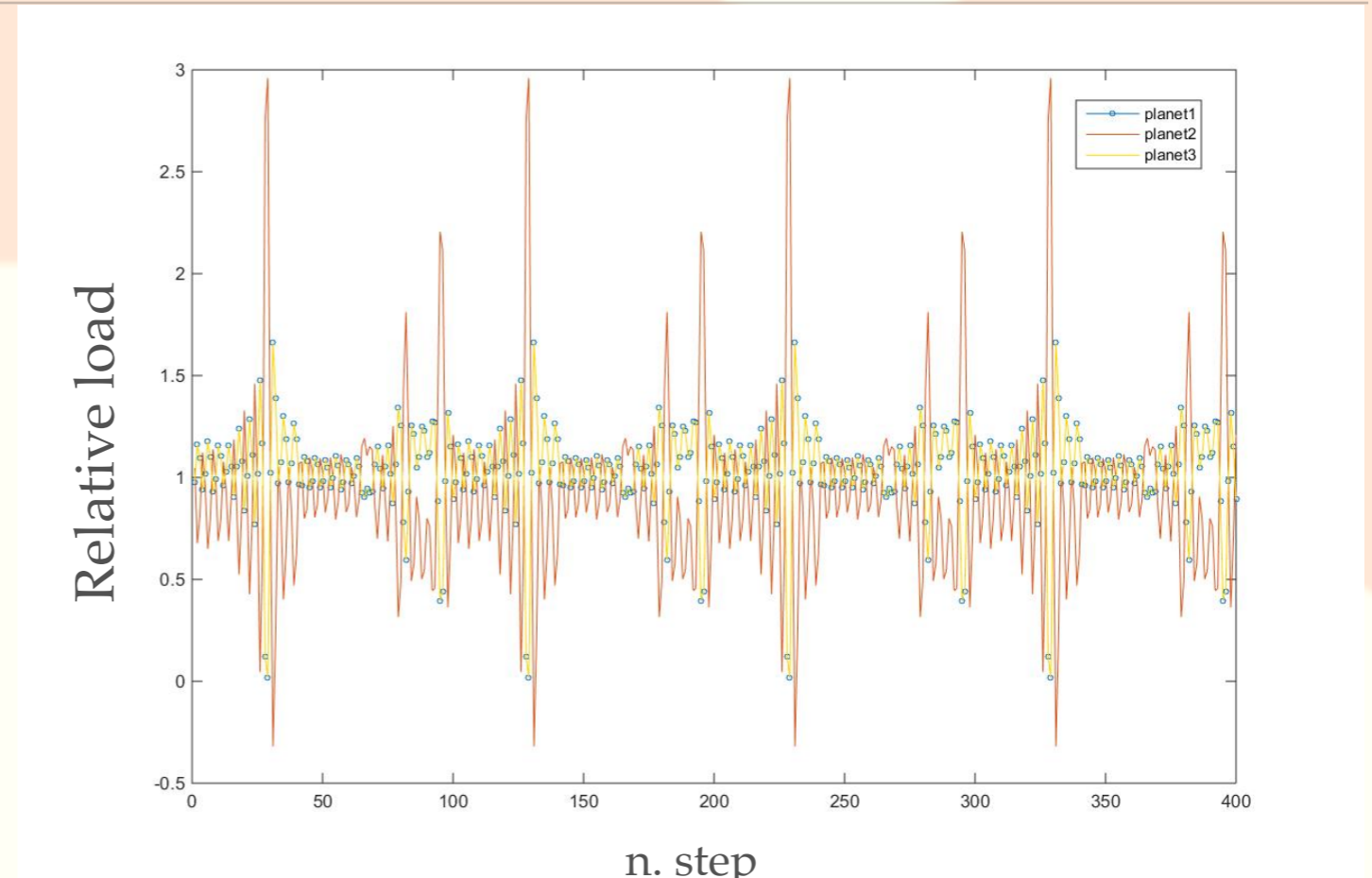
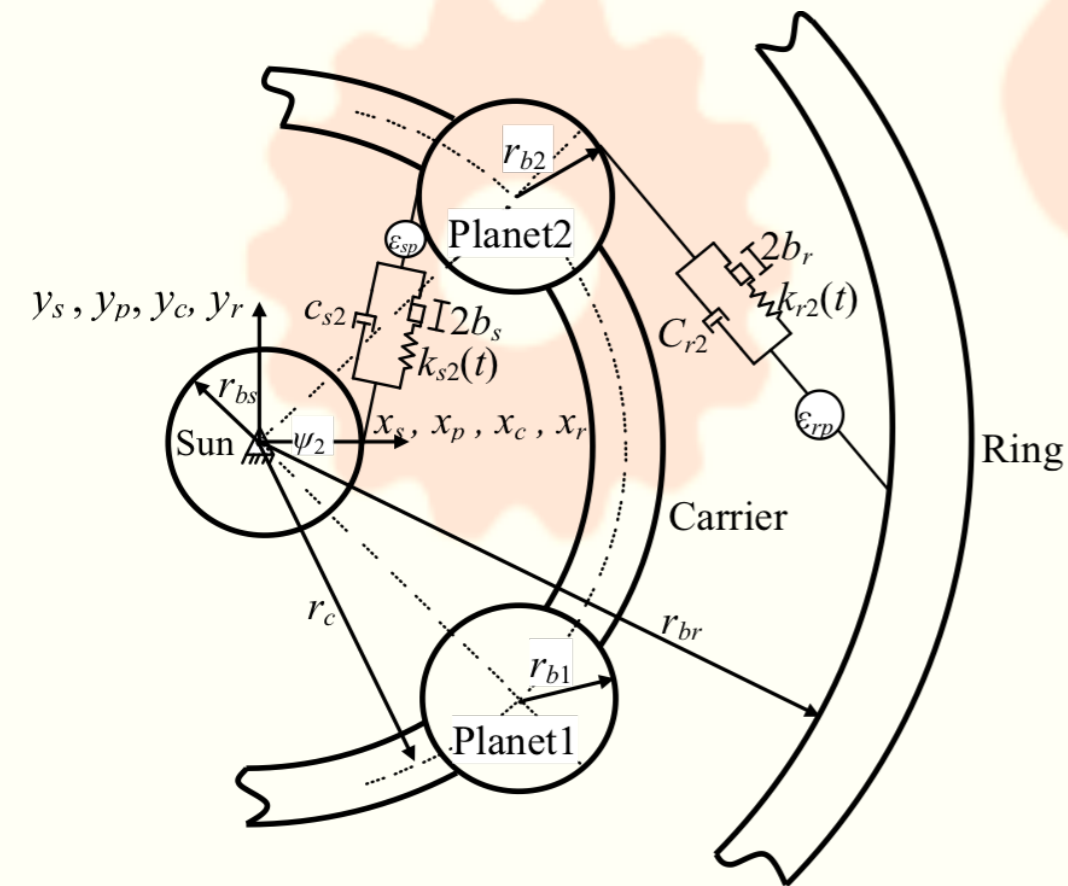
- ❖  $\hat{\psi}_n, cd, \hat{\alpha}_{s/r}$  are to be modified accordingly to the presence of errors
- ❖ Planet pin positioning errors are the more relevant



$$\begin{pmatrix} r_n \\ t_n \end{pmatrix} = \begin{pmatrix} \cos \psi_n & \sin \psi_n \\ -\sin \psi_n & \cos \psi_n \end{pmatrix} \begin{pmatrix} x_n \\ y_n \end{pmatrix}$$



# Evaluating Load Sharing Coefficient



- ❖ 200  $\mu\text{m}$  error planet 2
- ❖ LS evaluation is performed for system with more planets

## 3 equally spaced planets

Load sharing factor	Planet1	Planet2	Planet3
Load-sharing (sun-planet)	0.3436	0.3128	0.3436

## 4 equally spaced planets

Load sharing factor	Planet1	Planet2	Planet3	Planet4
Load-sharing (sun-planet)	0.2634	0.1476	0.2682	0.3208

# Load Sharing: next steps

- ❖ Further developments include:
  - ❖ An experimental validation of the proposed method, which can be performed by means of strain-gauges measurements
  - ❖ Optimization of planet phasing in order to reduce the AGMA mesh load factor  $K_\gamma$



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# Experiments on coated gears



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# Test rig for coatings/treatments on gears



- ❖ A test rig for gear pair dynamic measurement (courtesy of CNH) has been used for an experimental campaign

# Test planning

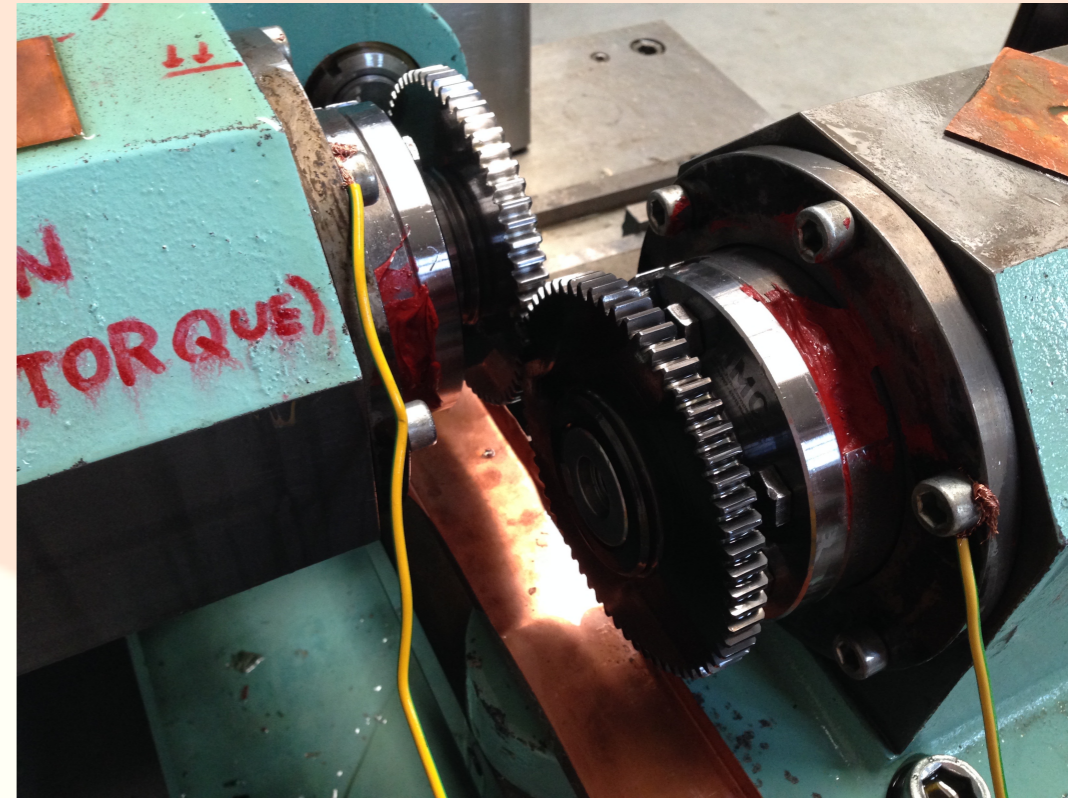
1-3	tempered	/	/
4-6	tempered	coating 1	/
7-9	tempered	coating 2	/
10-11	tempered	/	/
12-14	carburized	/	/
15-17	carburized	coating 1	/
18-20	carburized	coating 2	/
21-23	carburized	/	texturing 1
24-26	carburized	/	texturing 2
27-29	nitrided	/	/
30-32	nitrided	coating 1	/
33-35	nitrided	coating 2	/

- ❖ Gears with three kinds of thermal treatment are considered
- ❖ For each thermal treatment, two different kinds of Tungsten Carbide / Carbon (WC/C) coatings and the uncoated case are investigated
- ❖ Some gears have been left for surface texturing (to be tested)
- ❖ An equivalent set of tribometer disks have been produced (using the same steel)

# Test planning

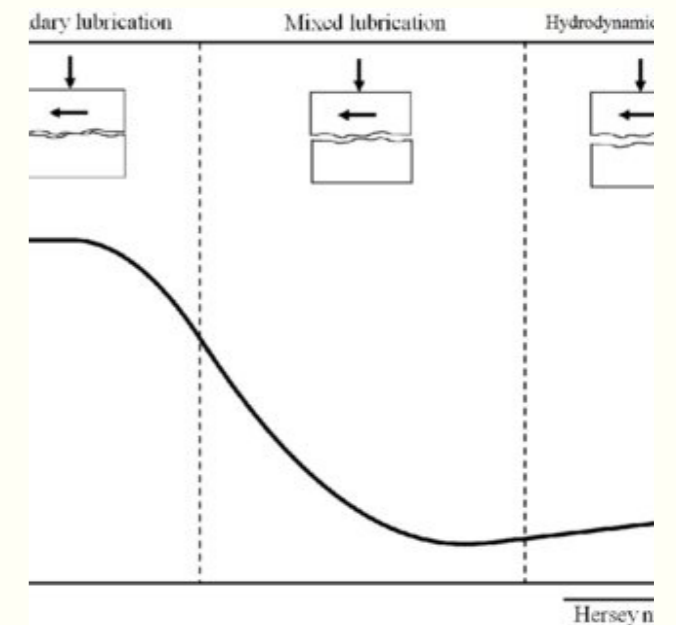
## Gear test

- ❖ Rolling/sliding contact
- ❖ Max pressure: 1.5 GPa (pure rolling)
- ❖ Max sliding speed: 2 m/s @ 0.8 Gpa
- ❖ Oil jet lubrication: Shell OMALA VG 68 (mineral)
- ❖ Efficiency curves will be measured



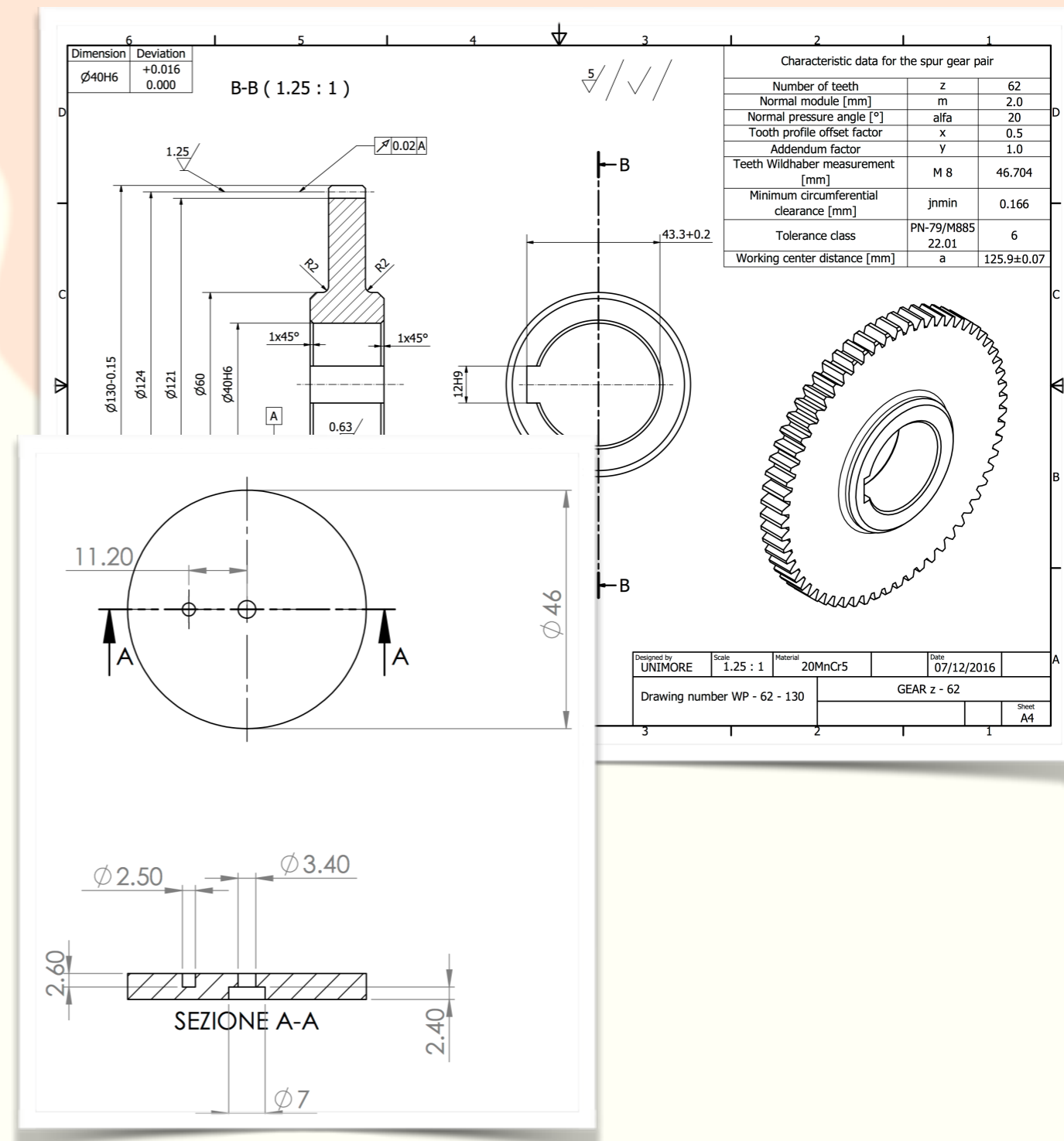
## Ball on disk tribometer

- ❖ Sliding contact
- ❖ Max pressure: 0.8 GPa
- ❖ Max sliding speed: 1.5 m/s
- ❖ Stribeck curves will be measured
- ❖ Dip lubrication: VG 68 LT or VG 150 HT
- ❖ Pure sliding will result in less hydrodynamic lift

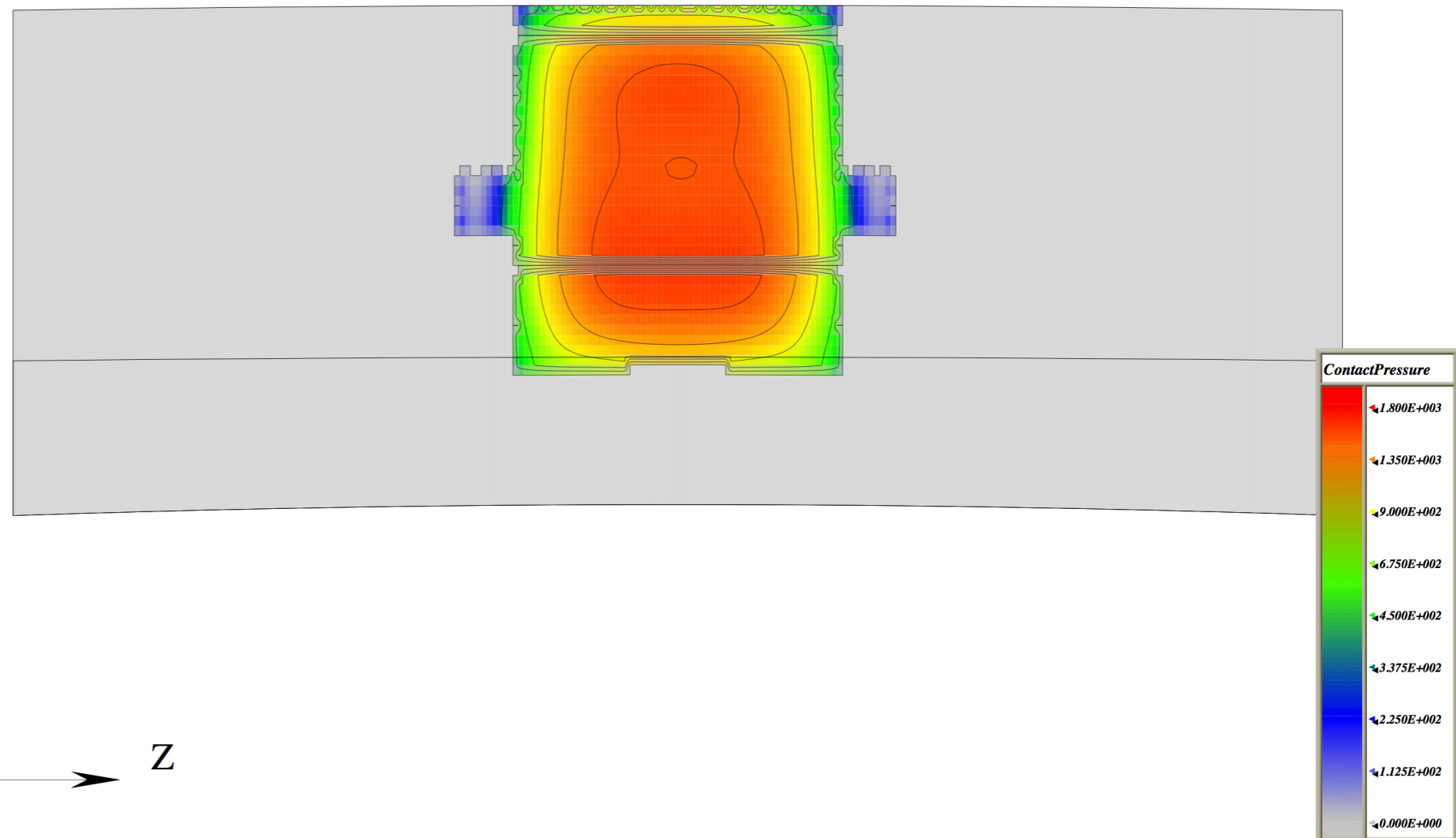
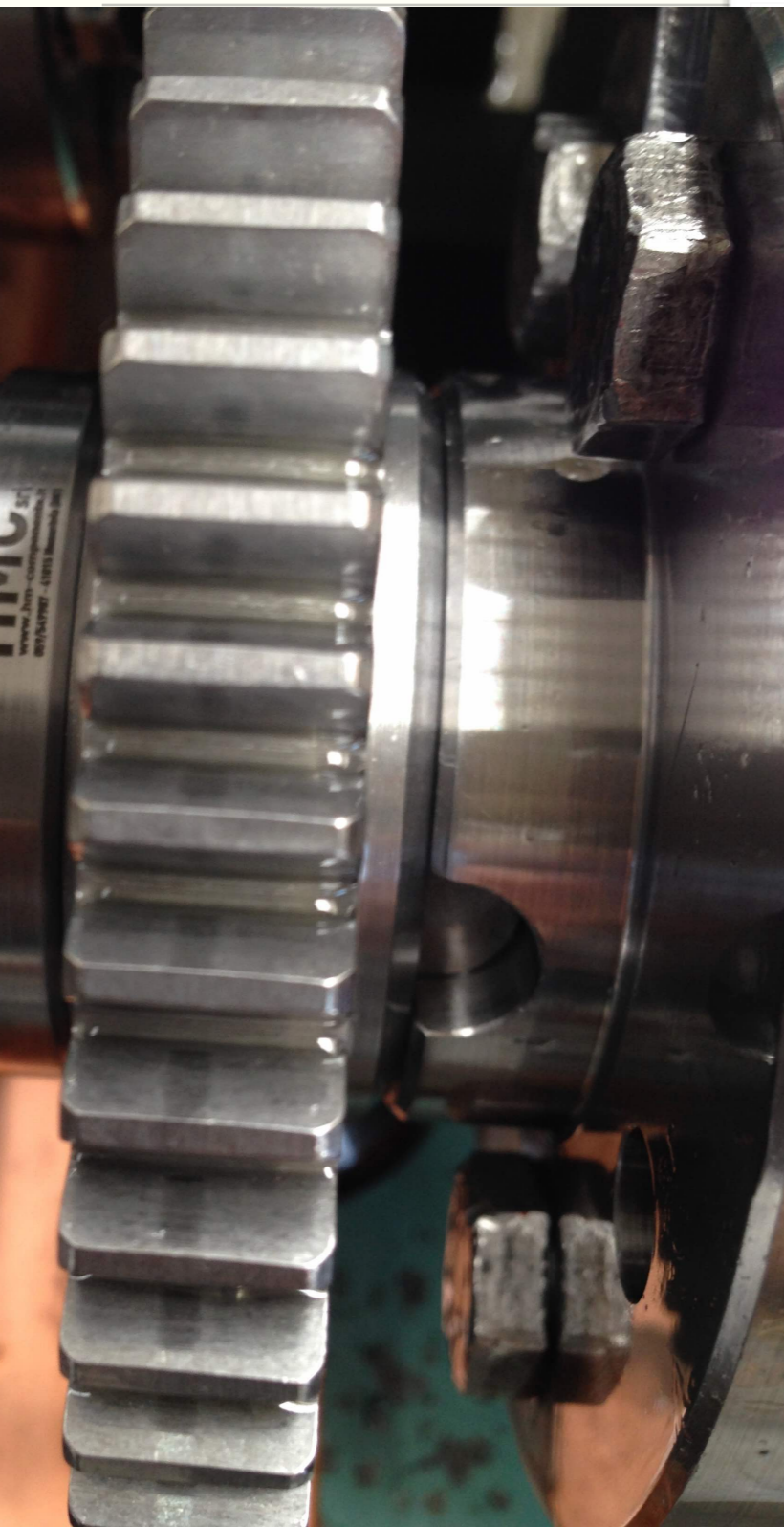


# Gear sample design

- ❖ Spur gear  $z=62$ ,  $m=2\text{mm}$ , 1:1 ratio
- ❖ Gears and tribometer disks are made using 20MnCr5 steel (suitable both for carburizing and nitriding)
- ❖ Thermal treatments are applied
- ❖ Both gears and disks are grinded (large crowning,  $100\mu\text{m}$ )
- ❖ Tumble finish is applied to both ( $R_a=0.2\mu\text{m}$ )
- ❖ WCC coatings are performed



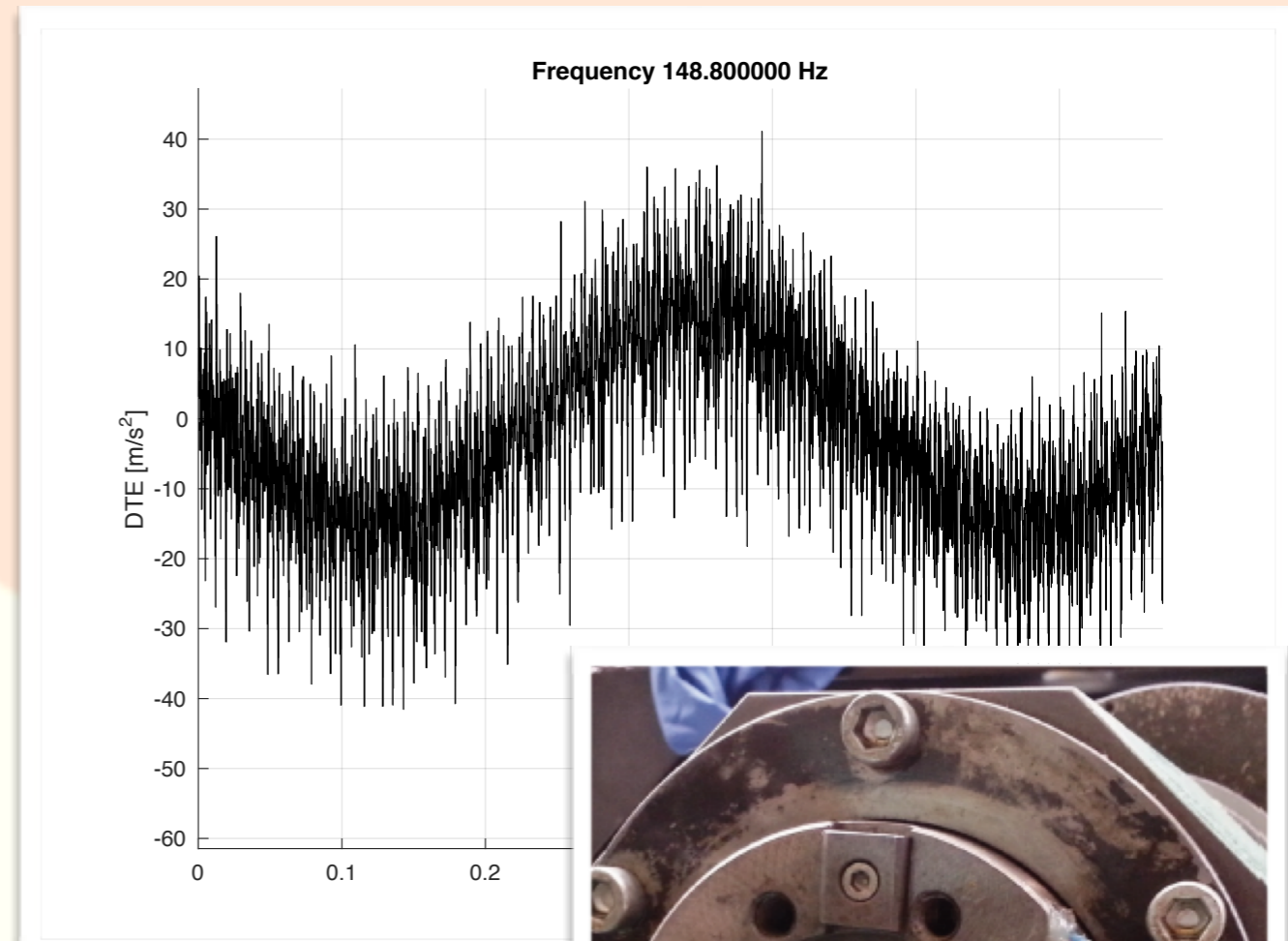
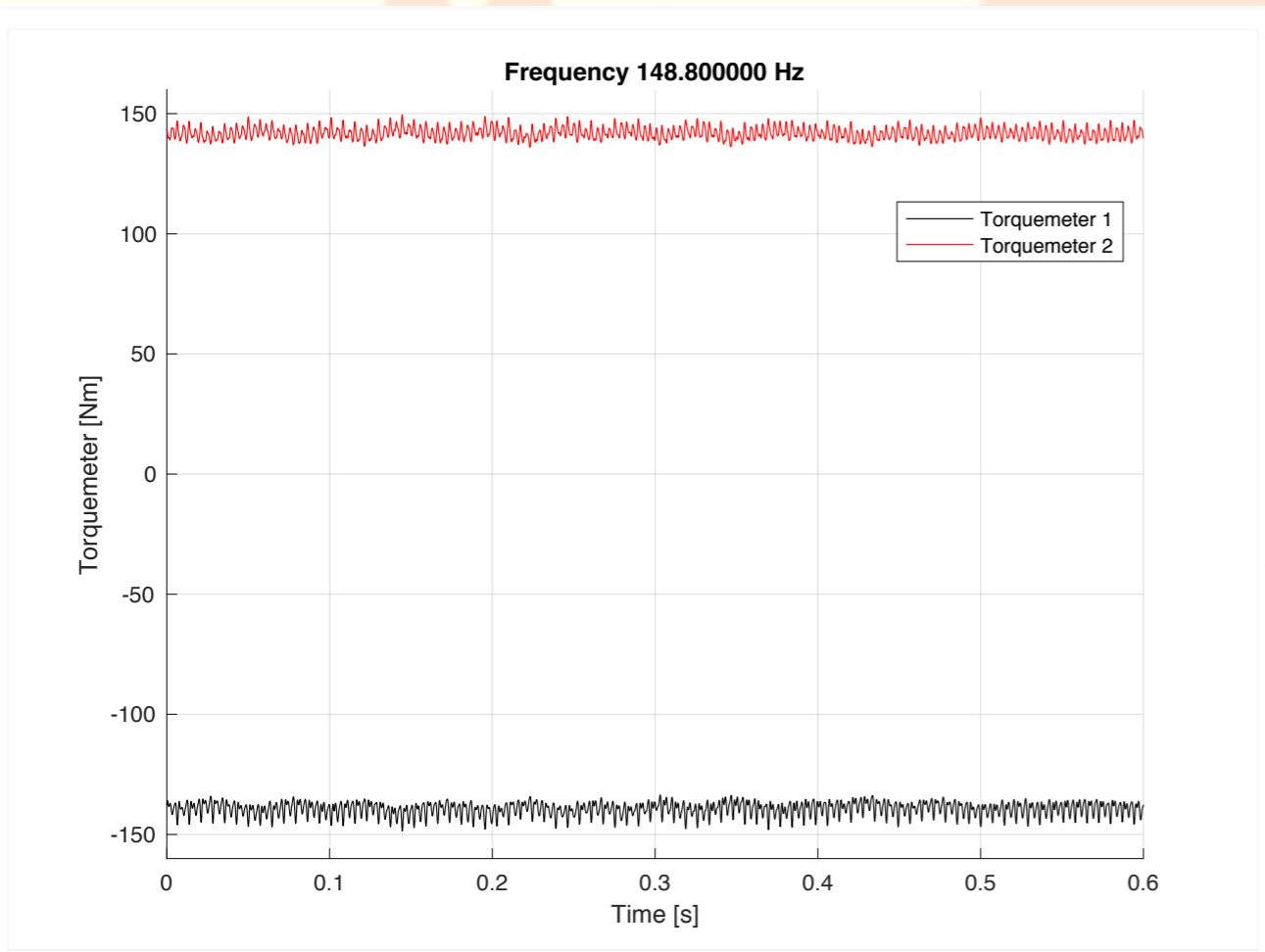
# Load conditions



- ❖ 62-62 gear pairs are tested
- ❖ Maximum allowable load 240 Nm
- ❖ Nominal load 150 Nm,  $p_h=1.5\text{GPa}$



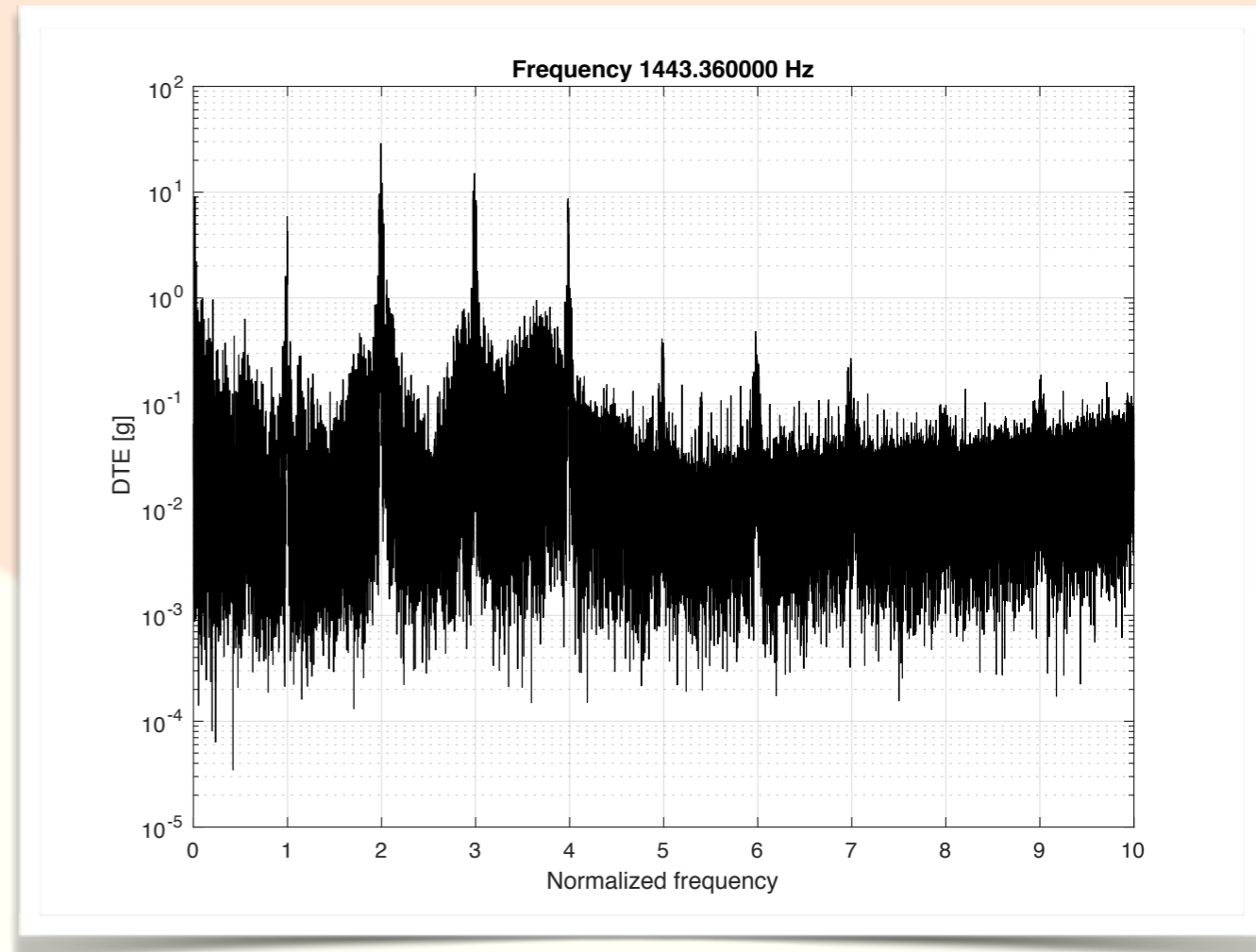
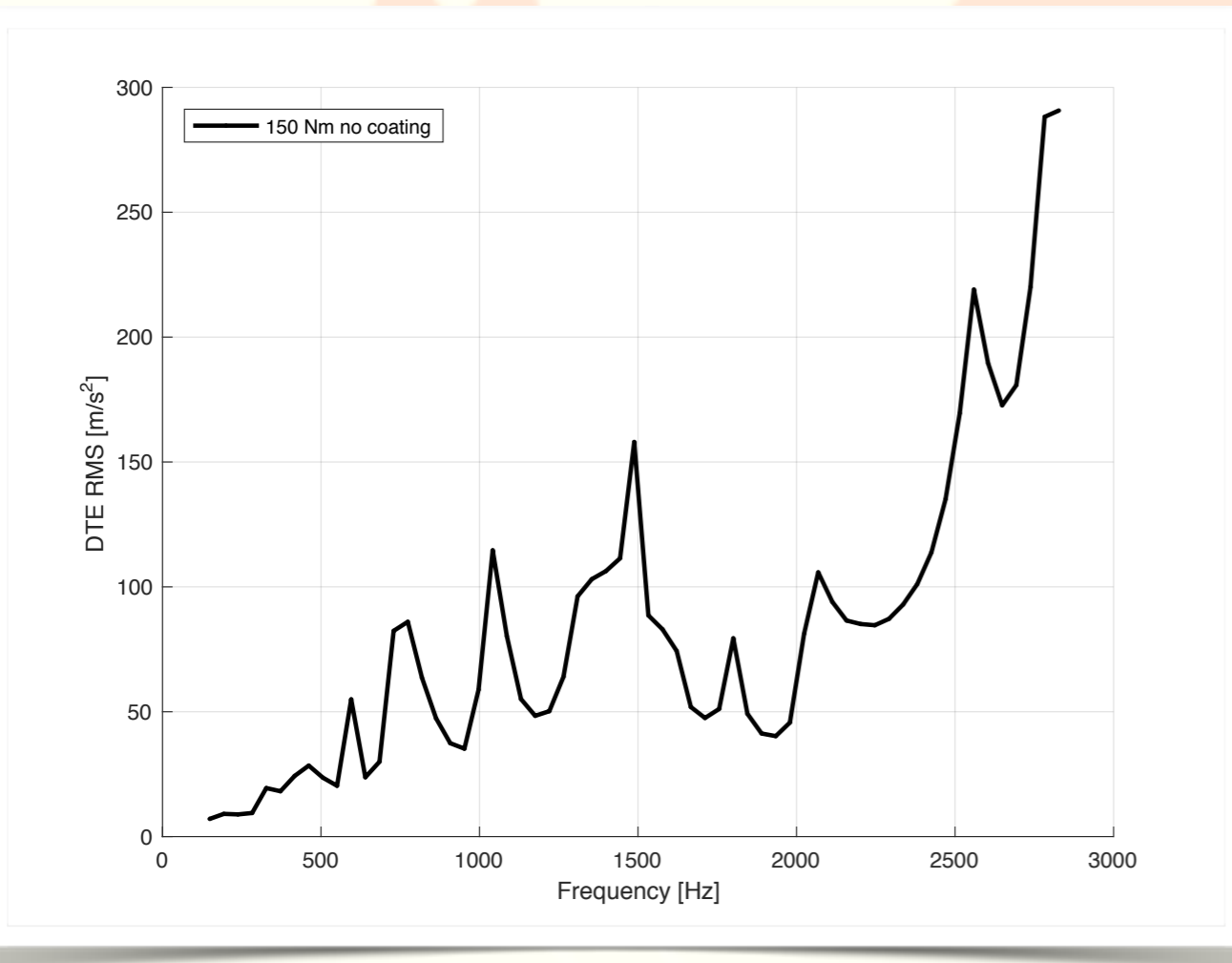
# Dynamic measurements



- ❖ Acceleration and torque signals are acquired simultaneously
- ❖ DTE is computed combining 4 acceleration signals

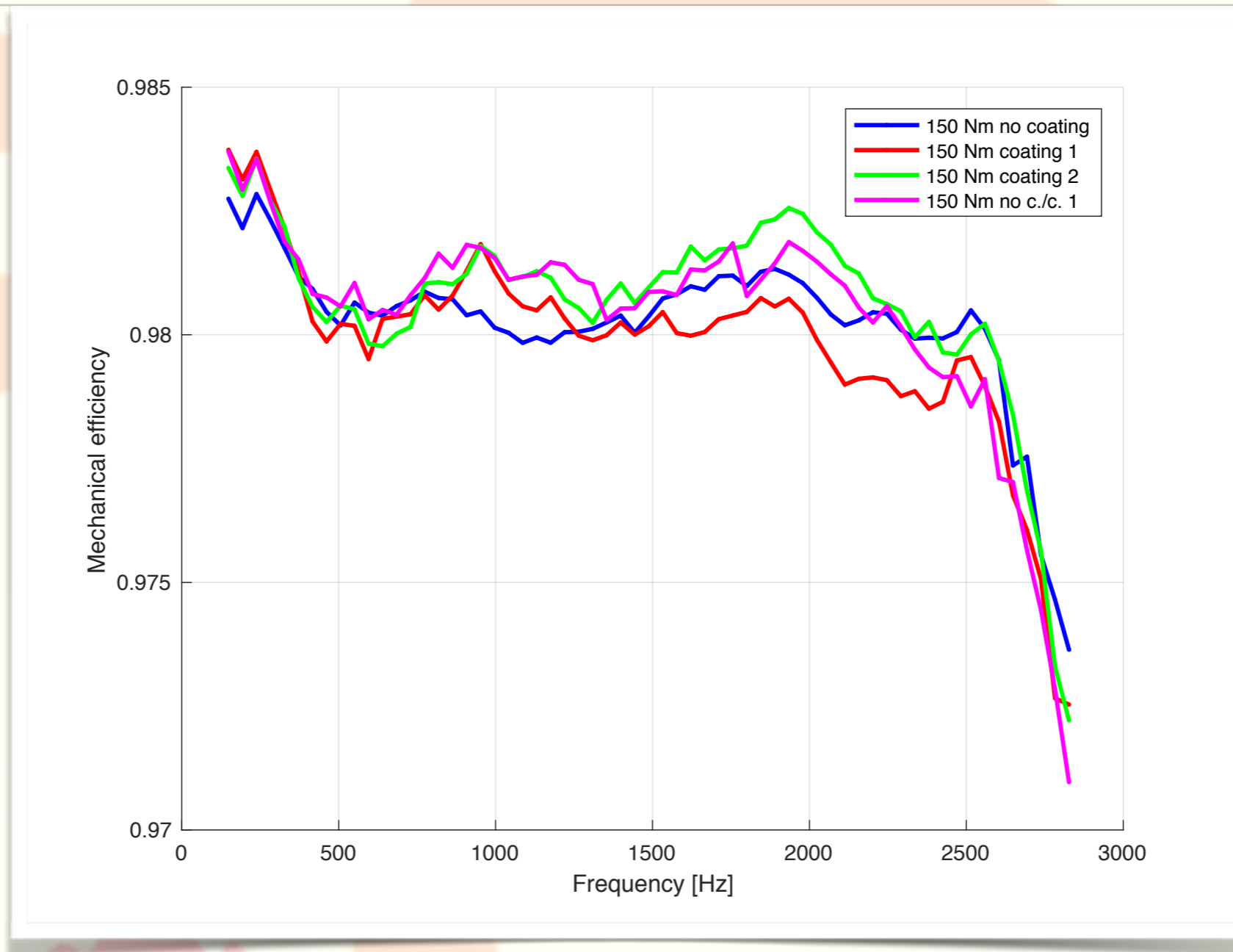
$$DTE = \frac{\ddot{x}_{11} + \ddot{x}_{12}}{2} \frac{R_{b1}}{R_{c1}} - \frac{\ddot{x}_{21} + \ddot{x}_{22}}{2} \frac{R_{b2}}{R_{c2}}$$

# Dynamic measurements



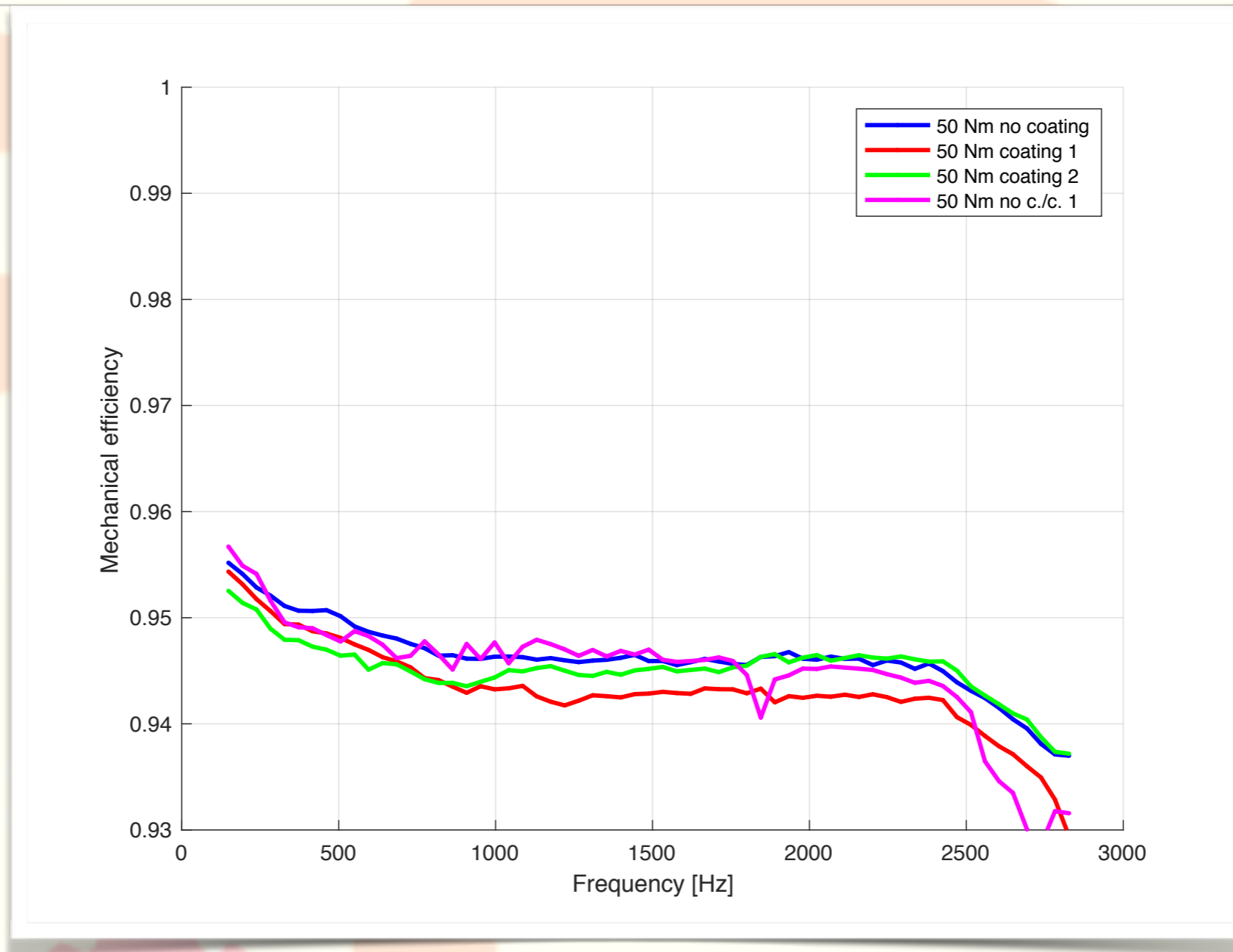
- ❖ 61 mesh frequencies (144-2736 RPM at pinion)
- ❖ Each speed lasts for 40 s (10 s acquisition)
- ❖ Efficiency is evaluated thanks to the torquemeters
- ❖ All gears are carburized

# Efficiency 150 Nm



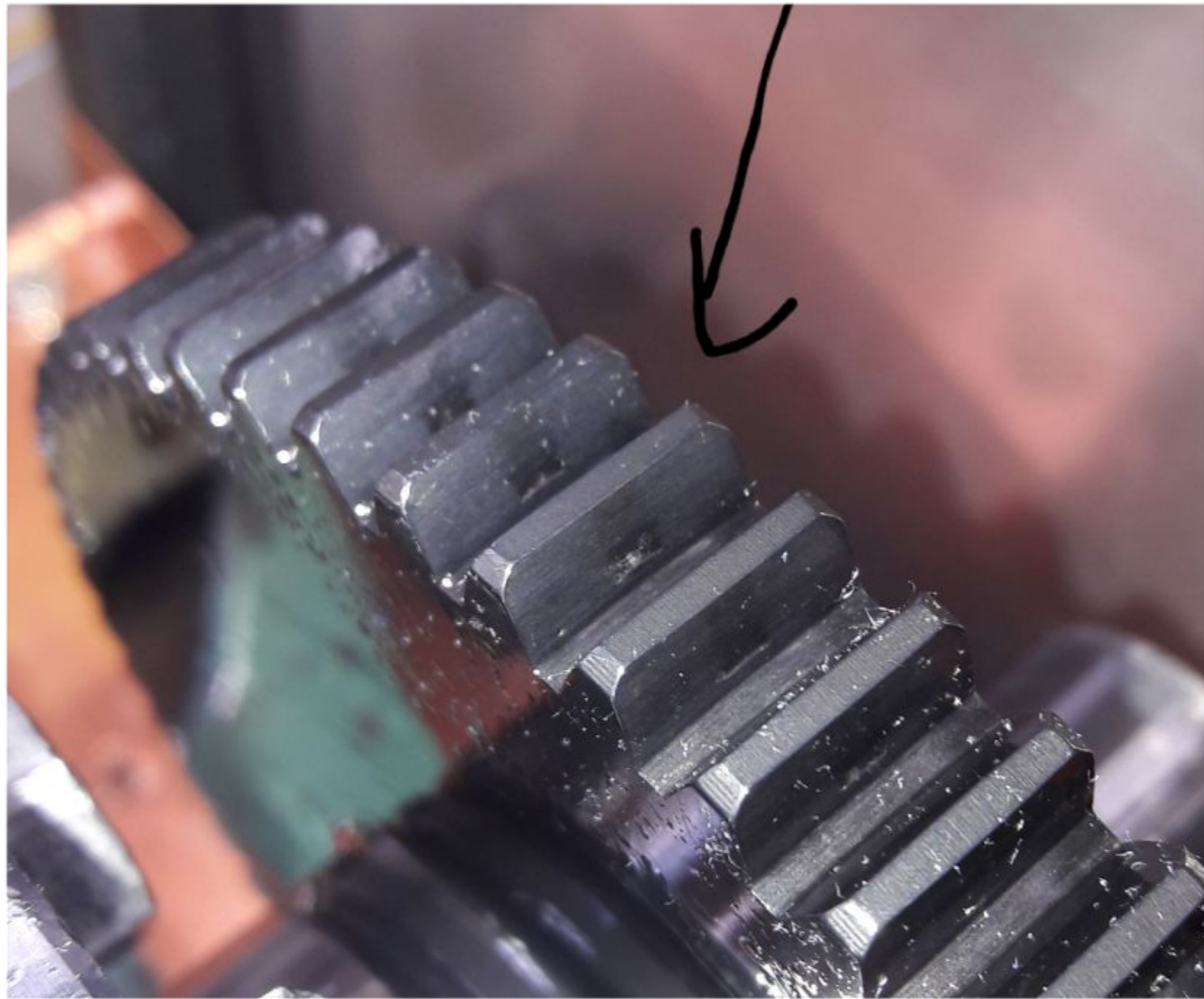
- ❖ Coating 1 and Coating 2 + Carburized are more efficient at the nominal torque
- ❖ At low speed Coating 2 and Coating 2 + Carburized are the most efficient

# Efficiency 50 Nm



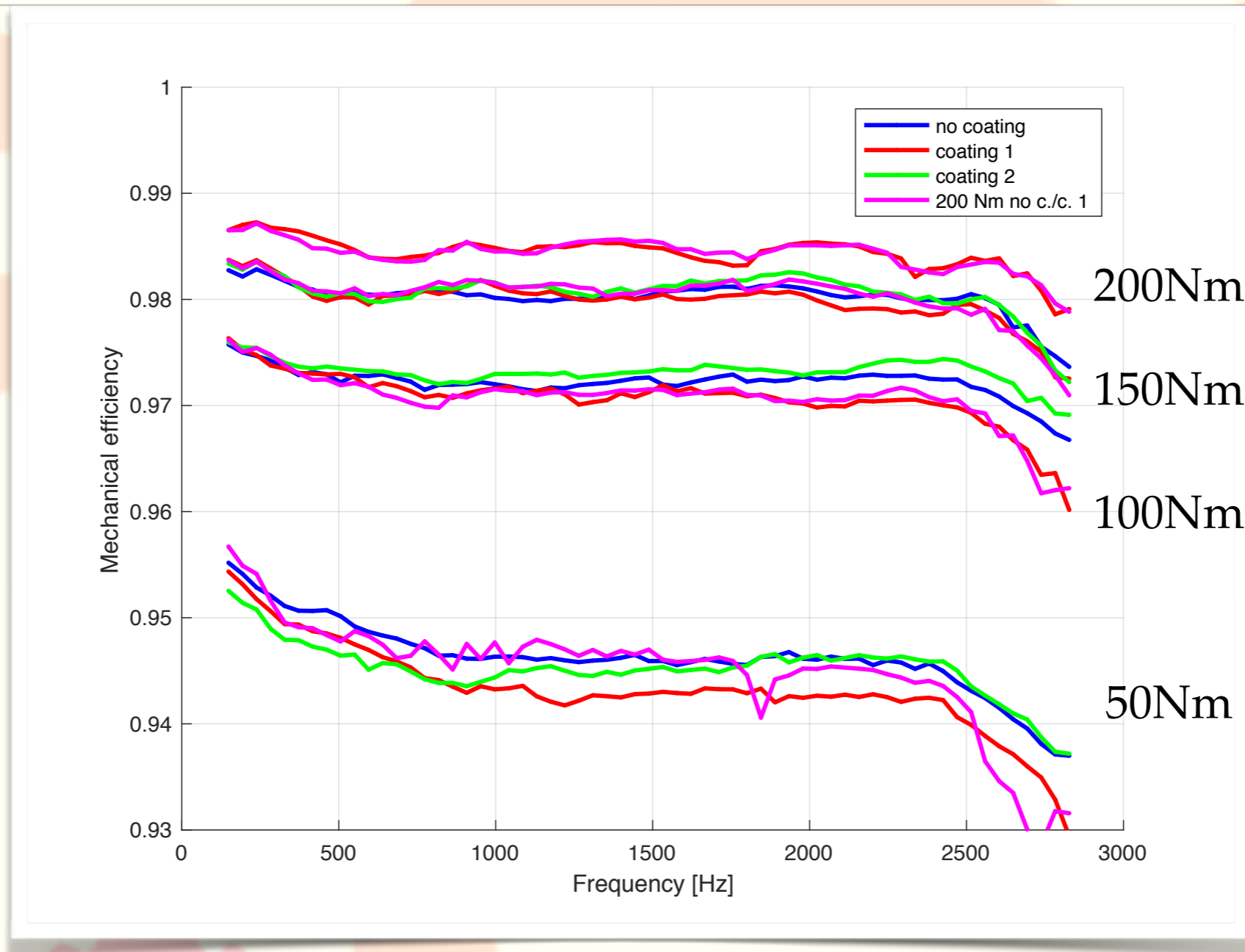
- ❖ Coating 1 and Coating 2 + Carburized are as much efficient as uncoated

# Coating 2 failure



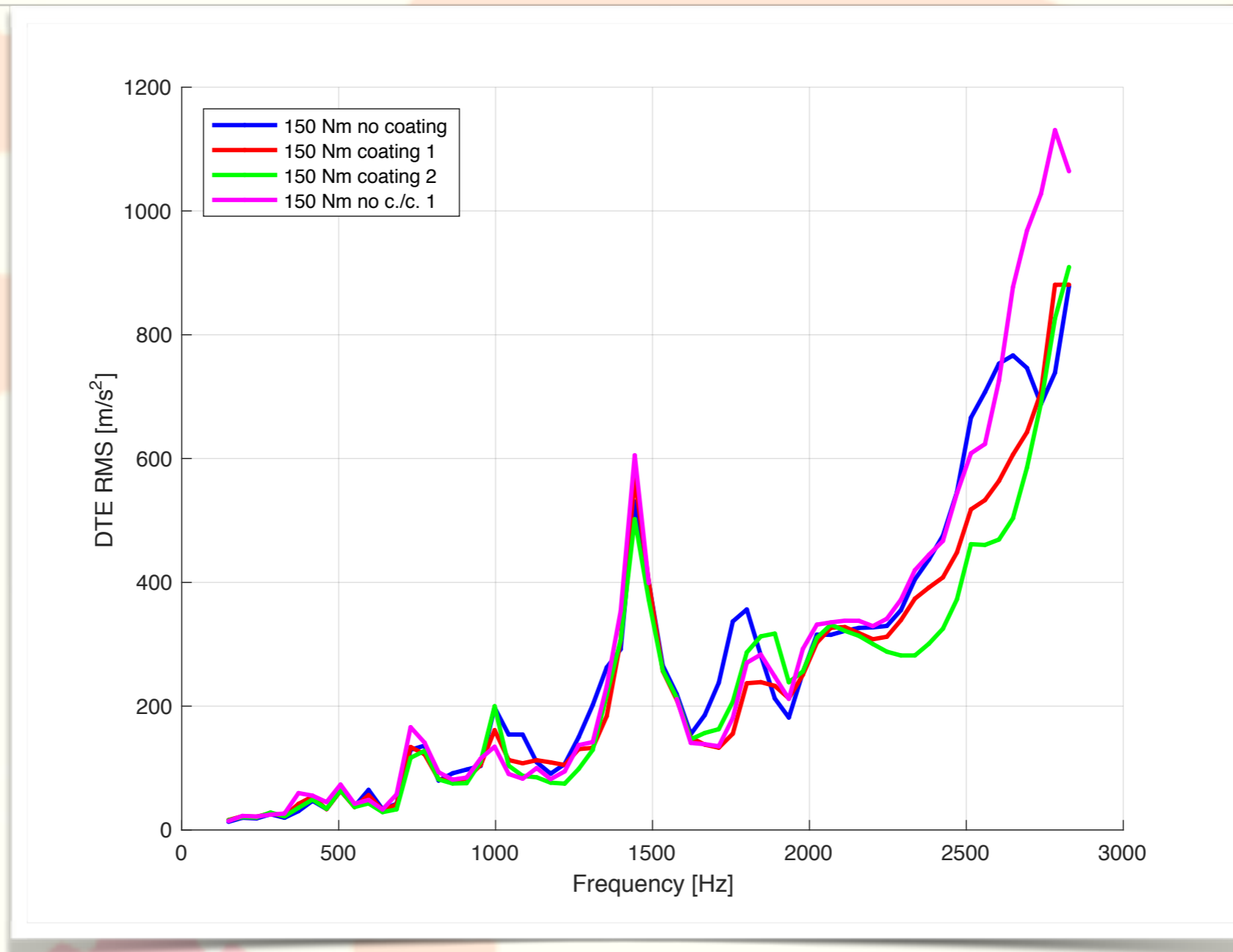
- ❖ Coating 2 failure occurs at 150 Nm
- ❖ WCC delamination is found close to the tip and root (failure mode: friction, low pressure)

# Efficiency comparison



- ❖ Coating 1 and Coating 1 + Carburized are reliable up to 200 Nm
- ❖ As expected, efficiency increases with torque (churning losses are less relevant)

# Efficiency comparison



- ❖ Coating 2 reduces vibrations in the gear pair, while coating 1 increases vibration levels
- ❖ Coating 1 + Carburized is the most noisy test case

# Conclusions

- ❖ A comparative test for gear coatings and treatments has been set-up
- ❖ Tested WCC show slight efficiency increase with respect to uncoated cases
- ❖ Efficiency increase generally produces larger vibration amplitudes
- ❖ Optimal efficiency is given by a combination of coating 1 and uncoated pair (coating 2 delaminates at 1.5 GPa)
- ❖ In the final part of the project, the role of superfinishing is going to be investigated (as well as surface texturing)





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