

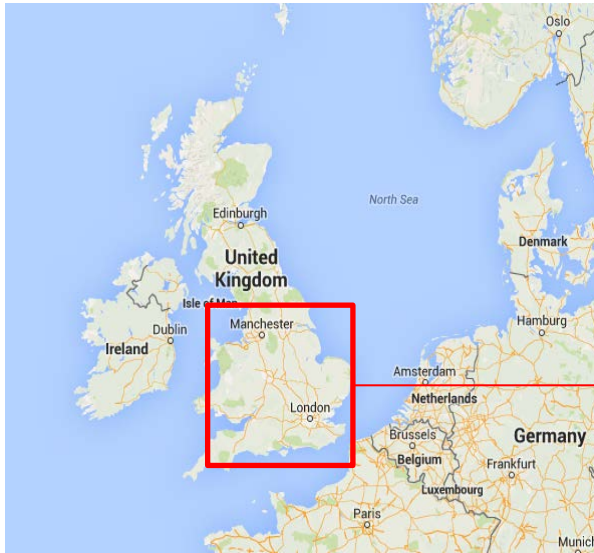


Loughborough  
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# Efficiency and Noise, Vibration and Harshness in systems transmitting power with gears

Stephanos Theodossiades

Dynamics Research Group  
Wolfson School of Mechanical, Electrical & Manufacturing Engineering  
Loughborough University  
United Kingdom

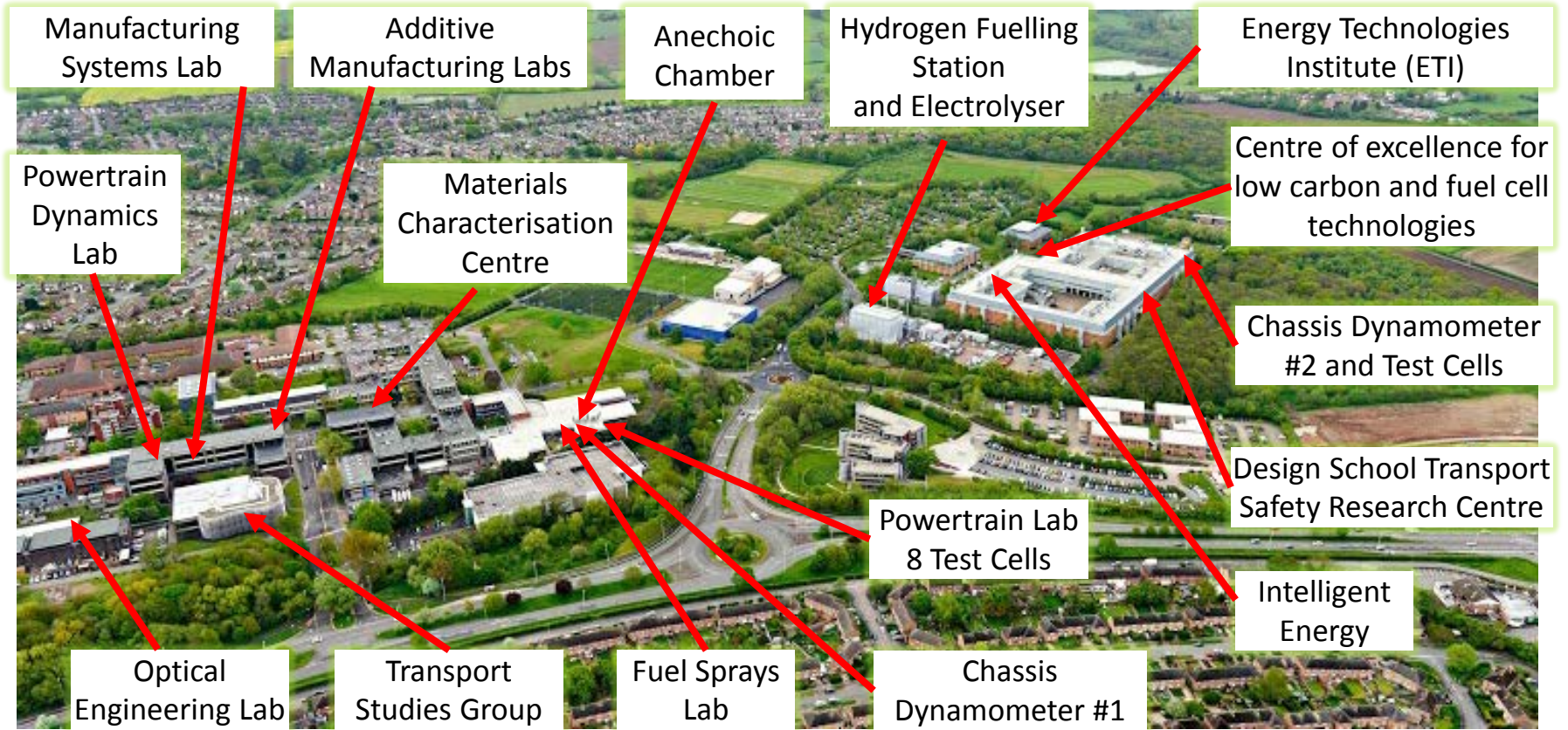


# About Loughborough University



- **7<sup>th</sup> position (The Complete University Guide 2017)**
- **13732 Full time Students**
- **1874 Part time Students**
- **763 Others – Full and Part time (Research exchange etc.)**

# Some Centres and facilities in the Loughborough University Campus



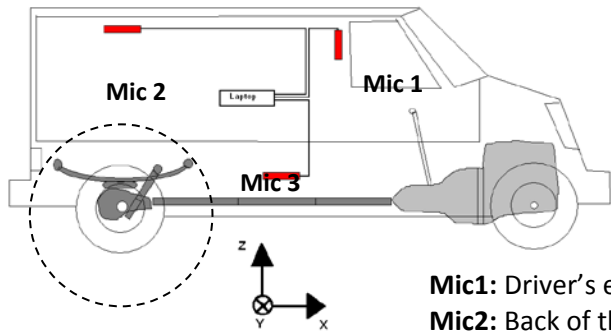
# Wolfson School of Mechanical, Electrical and Manufacturing Engineering

- **6<sup>th</sup> position (Complete University Guide 2017)**
- **1054 Full time Undergraduate Students**
- **162 Full time Postgraduate Students (MSc and PhD)**
- **35 Part time Undergraduate Students**
- **125 Part time Postgraduate Students (MSc and PhD)**
- **70 academic staff**
- **30 technical staff**
- **20 admin/secretarial staff**

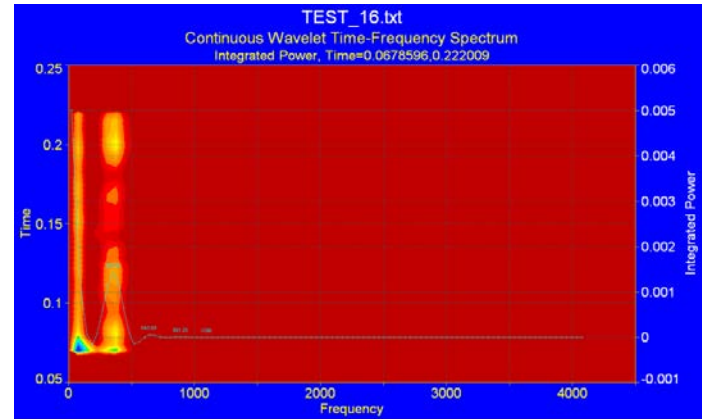


- **Problem definition (application: hypoid gears)**
- **Methodology**
- **Results**
- **Conclusions**
- **Published work**

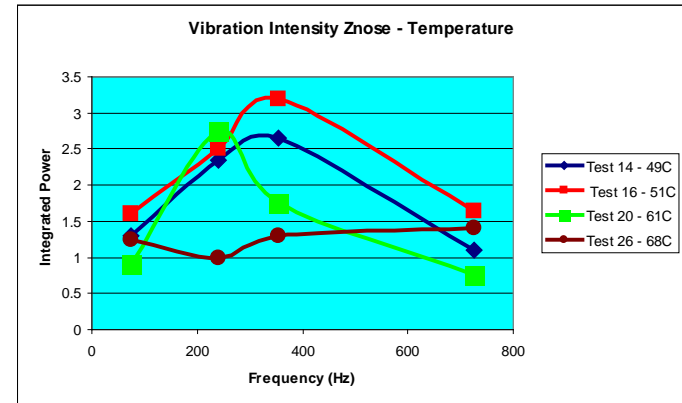
# Problem definition



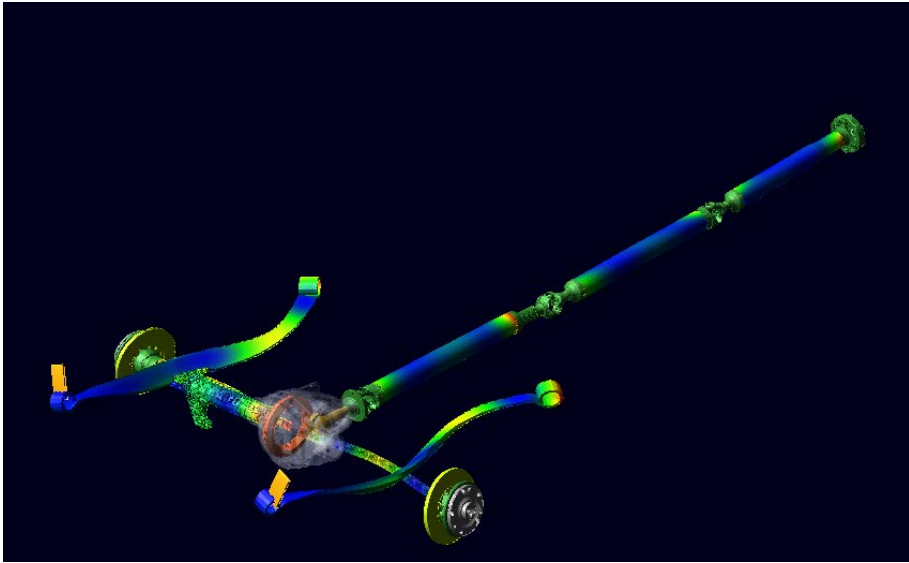
**Mic1:** Driver's ear  
**Mic2:** Back of the cabin  
**Mic3:** Underbody of vehicle



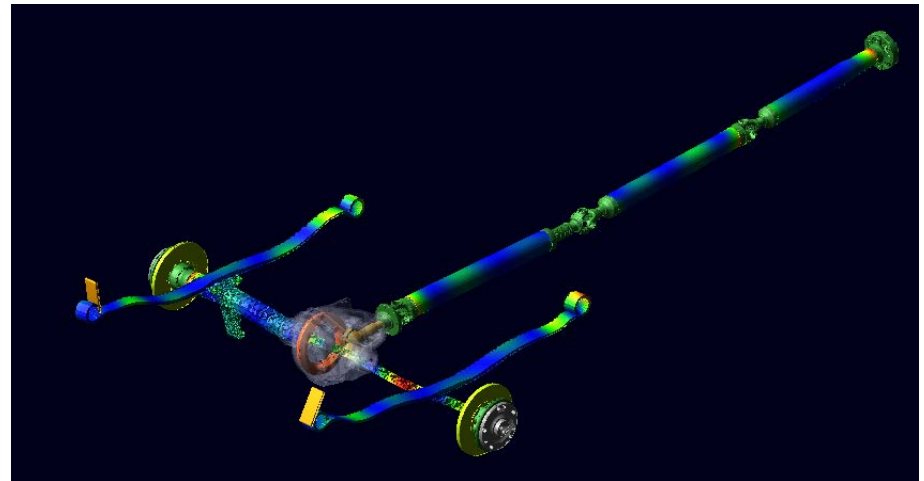
Wavelet of the rear cabin microphone signal



# Problem definition



**S-bend of leaf springs with twist of the rear axle (at 356 Hz)**

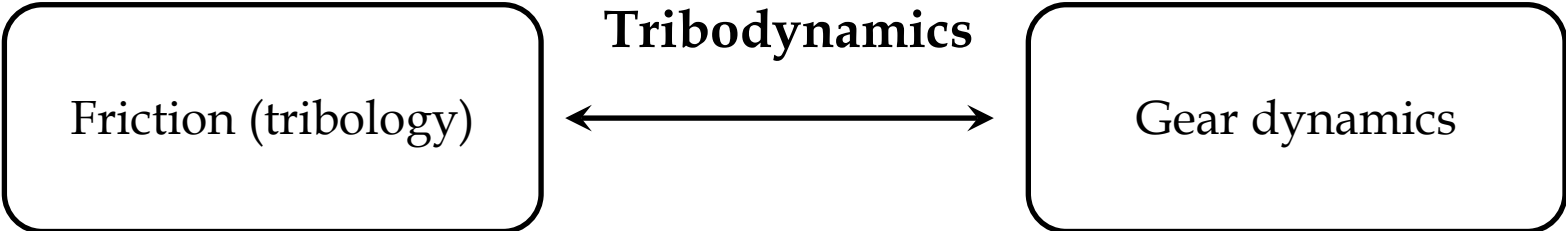
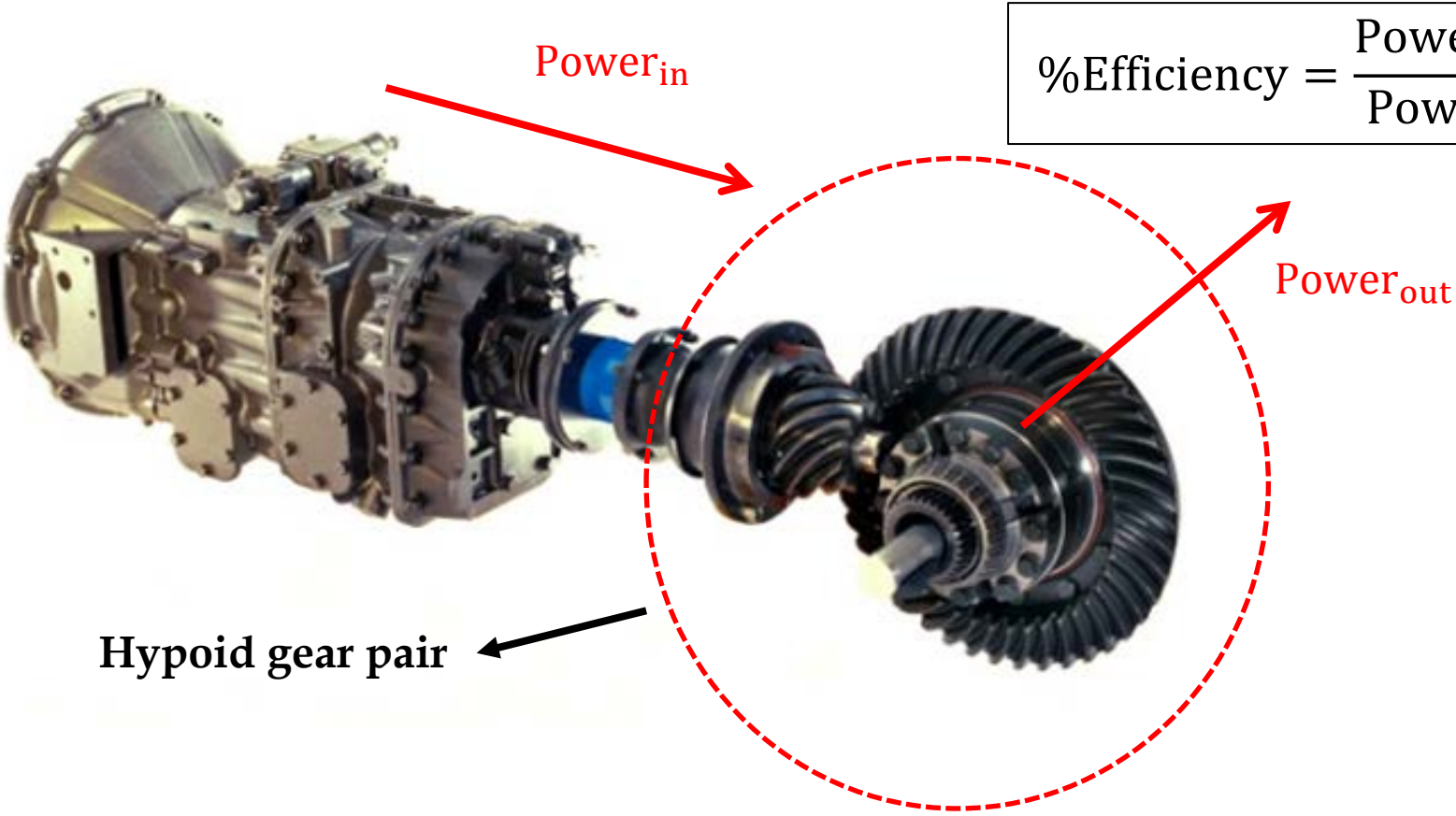


**Butterfly mode with multiple leaf spring bending (at 772 Hz)**



# Problem definition

$$\% \text{Efficiency} = \frac{\text{Power}_{\text{out}}}{\text{Power}_{\text{in}}} \times 100\%$$

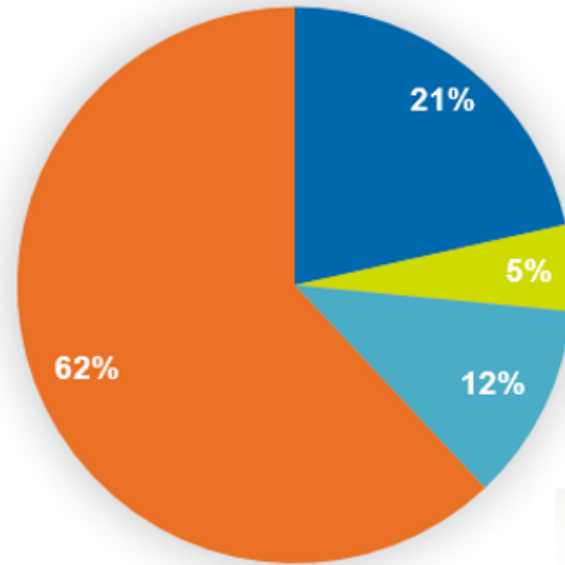
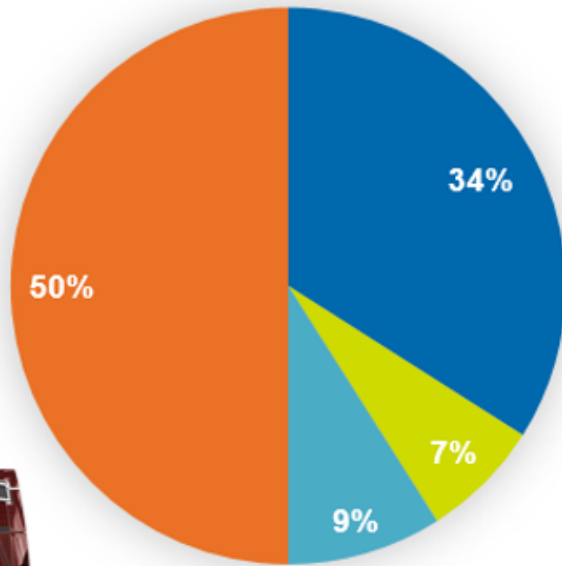


# Problem definition

## Energy Use

HD

PC

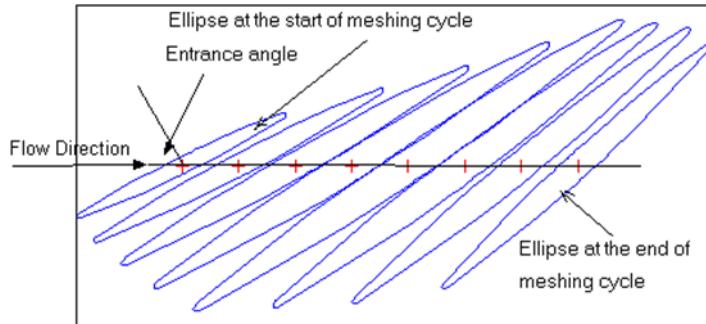
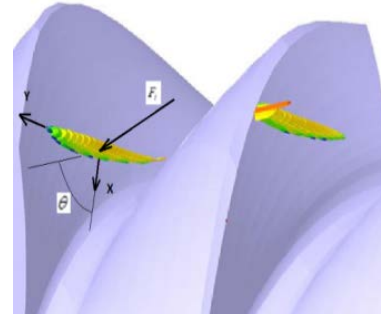


■ Energy used to move vehicle ■ Driveline ■ Engine ■ Thermal losses

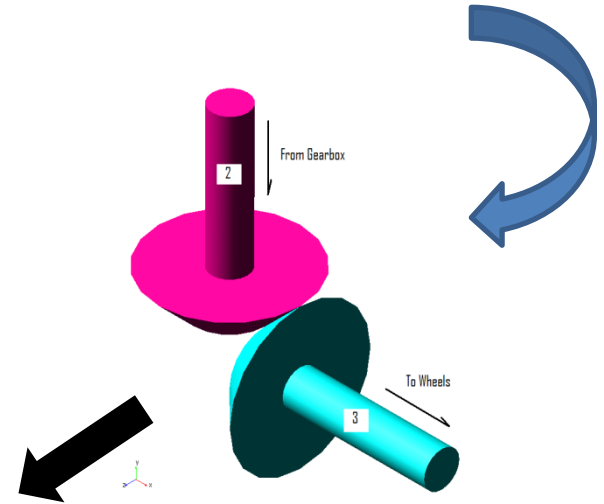
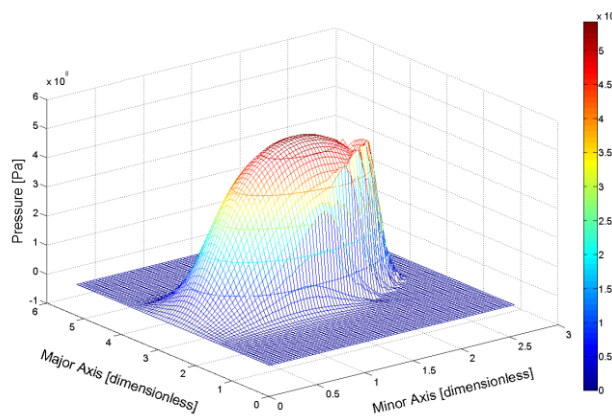


# Methodology

Gear geometry and assembly data



Elasto-hydrodynamic model

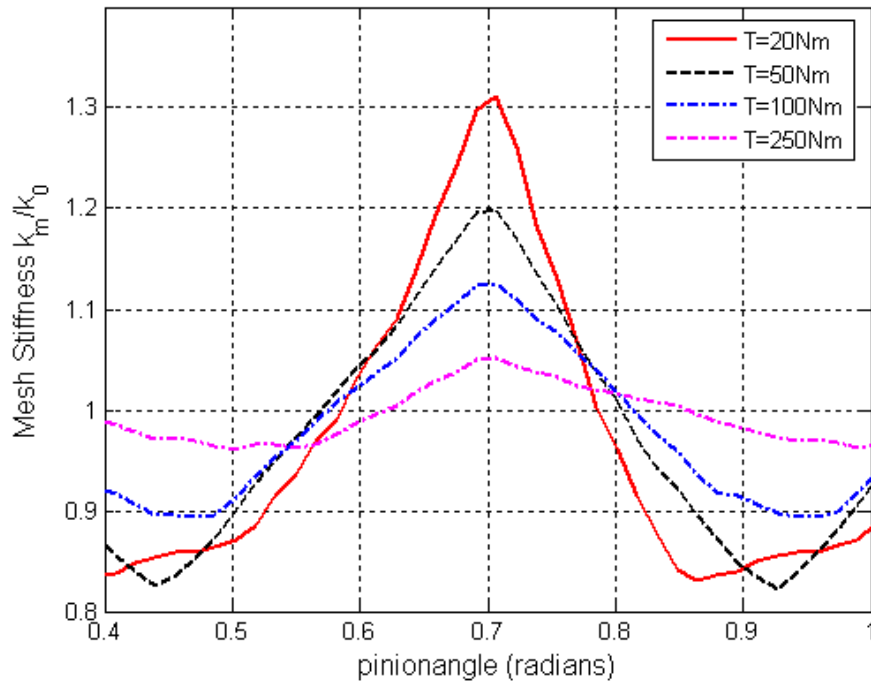


# Methodology - Hypoid gear pair contact geometry

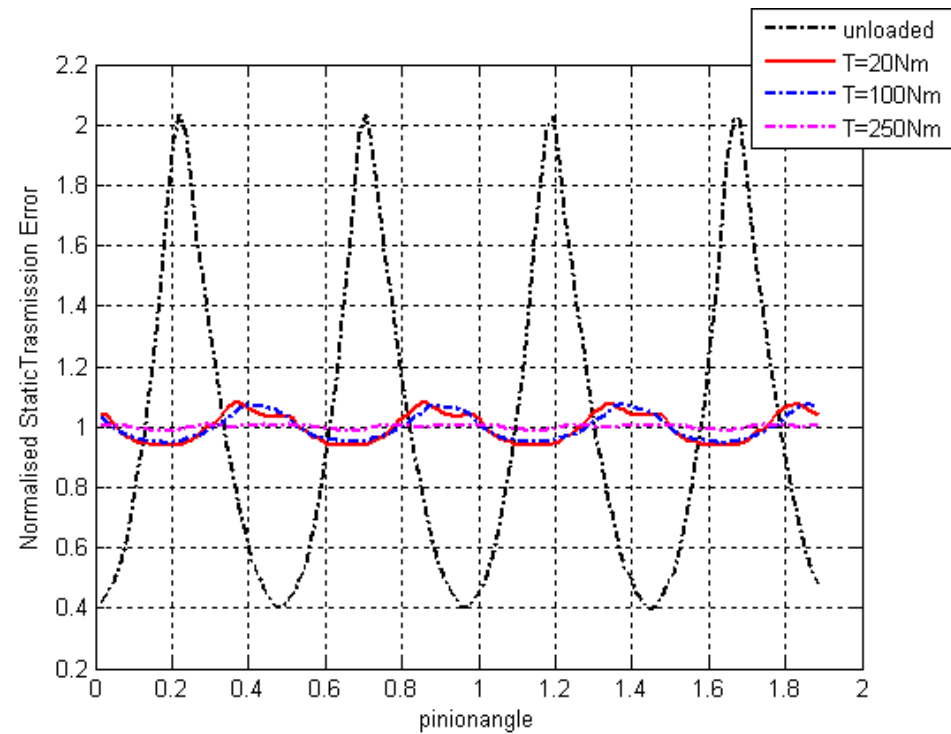
Tooth Contact Analysis  
(TCA):

- ✓ Numerical solution
- ✓ Commercial software  
CALYX
- ✓ Contact  
geometry/kinematics

# Methodology - Teeth meshing properties (I)

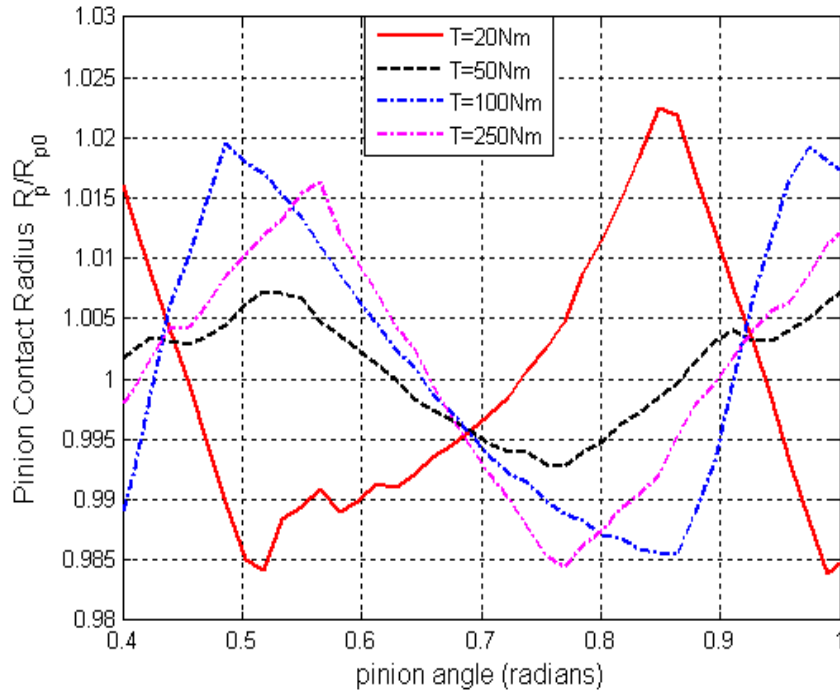


**Mesh Stiffness  $k_m$**

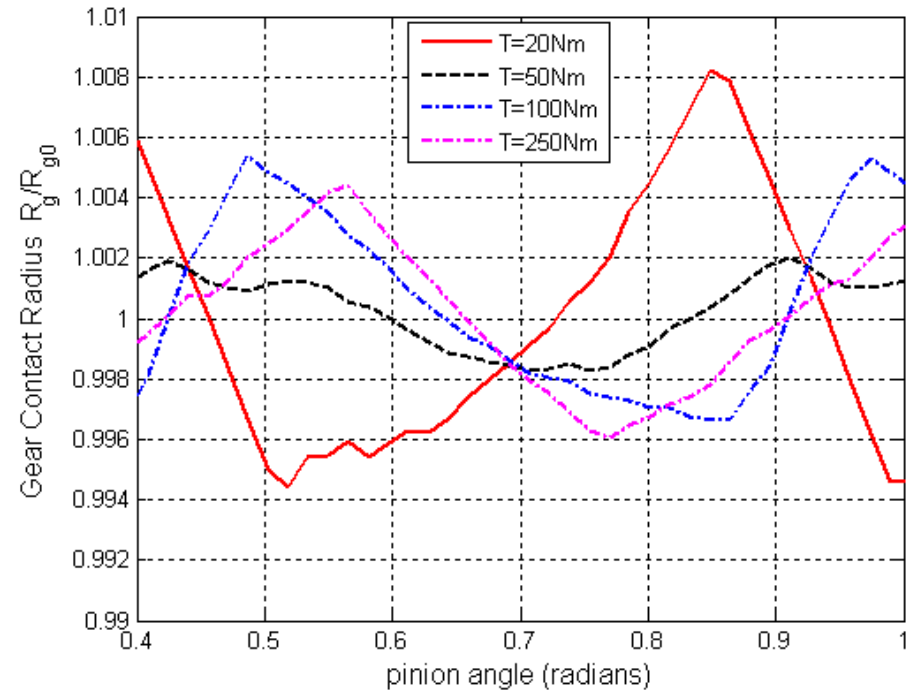


**Static Transmission Error**

# Methodology - Teeth meshing properties (II)



**Pinion Contact Radius**



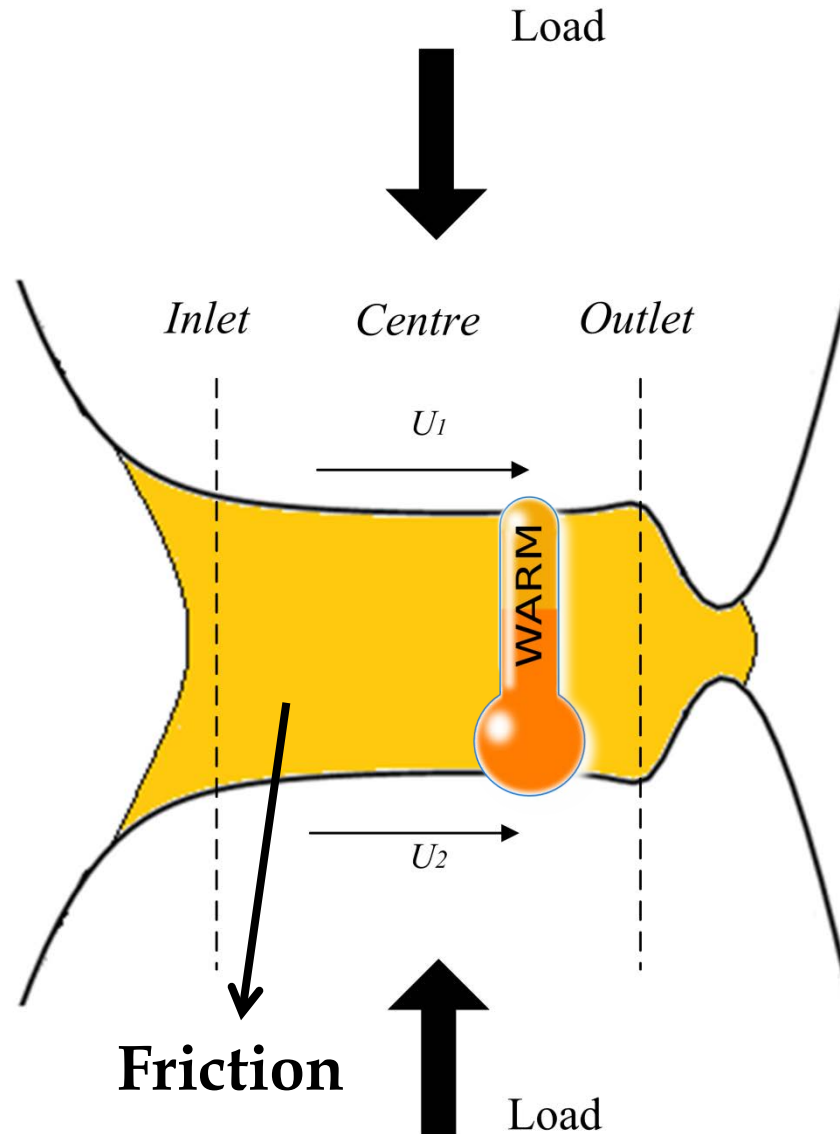
**Gear Contact Radius**

# Methodology - Elastohydrodynamic (EHD) regime of lubrication

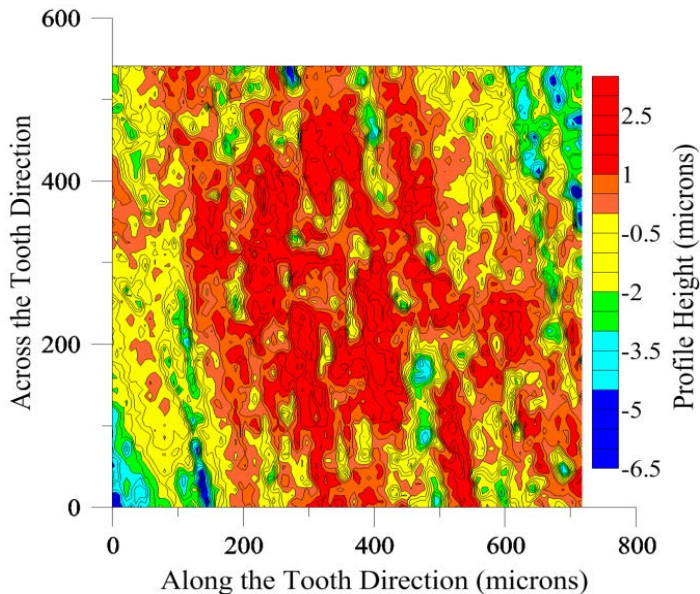
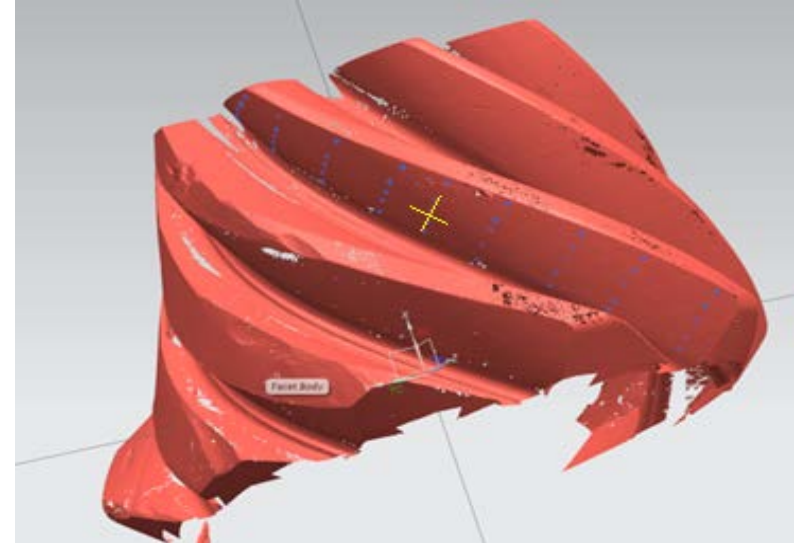
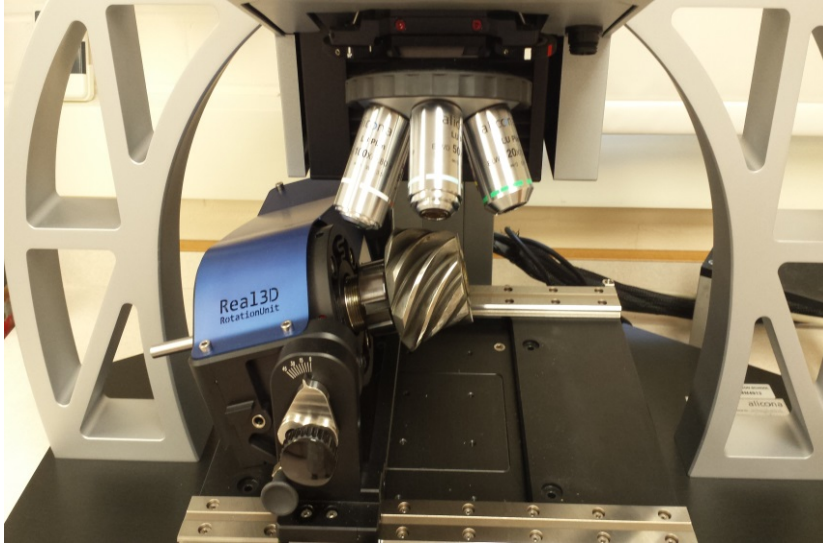
## Variation of viscosity with

- Pressure
- Shear rate
- Temperature

## Friction Model (viscous)



# Methodology - Friction Model (boundary)

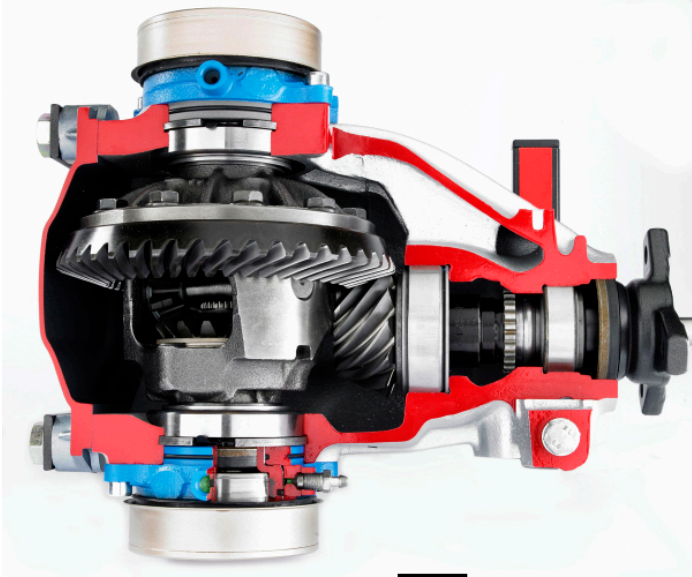


Asperity friction:

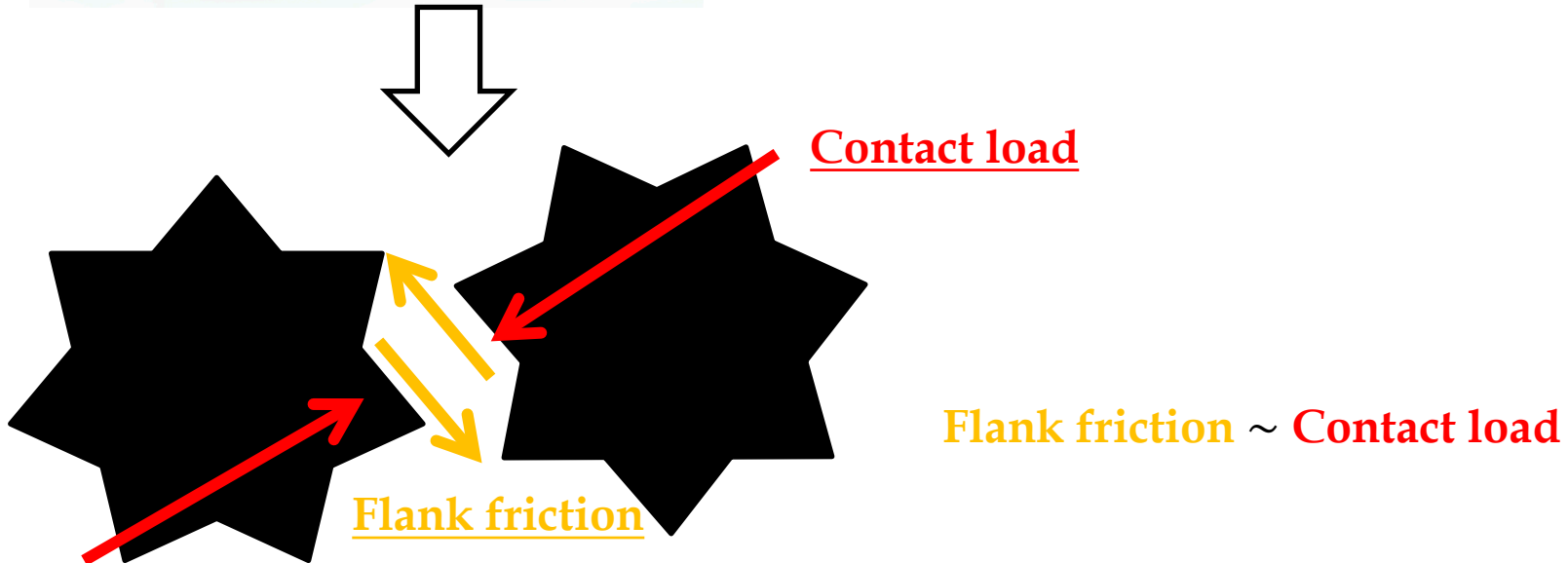
- Surface scan of gear teeth
- Surface model of the teeth
- Distribution of the asperity heights



# Methodology - Gear dynamics

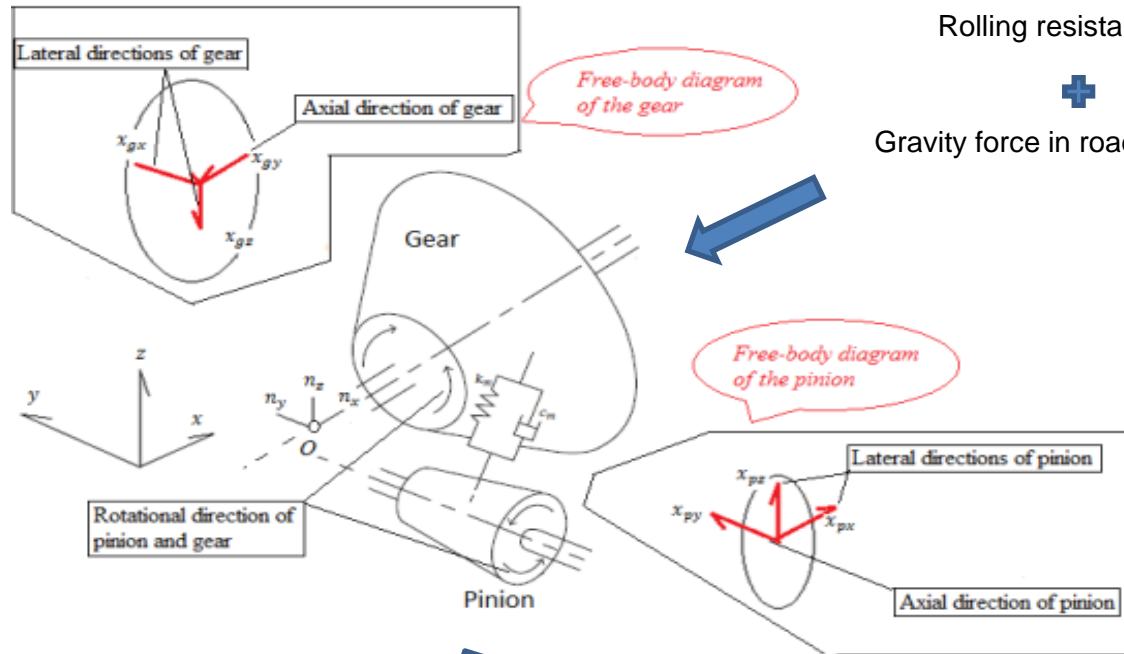


The gear dynamics (time varying contact load) causes fluctuations to the coefficient of friction and the power loss.



# Methodology - Gear dynamics

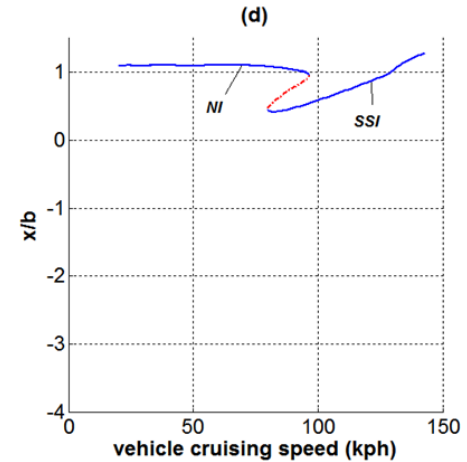
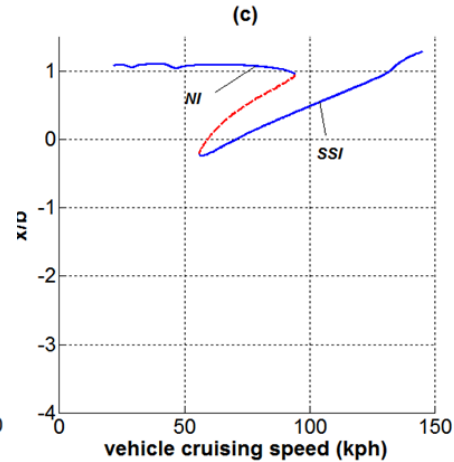
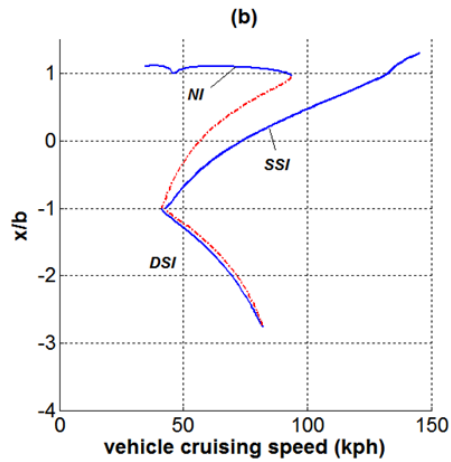
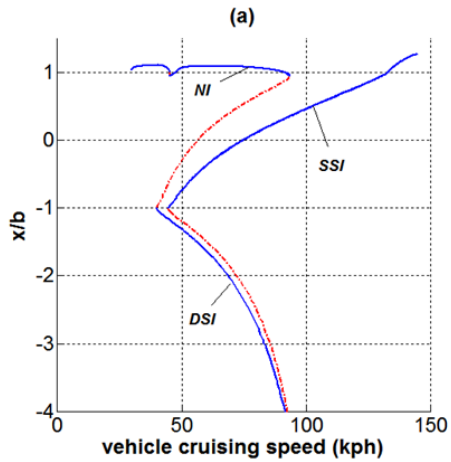
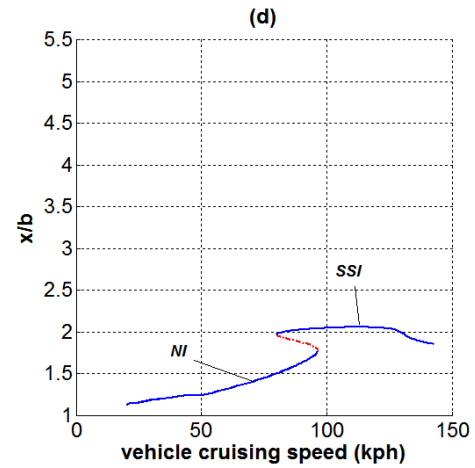
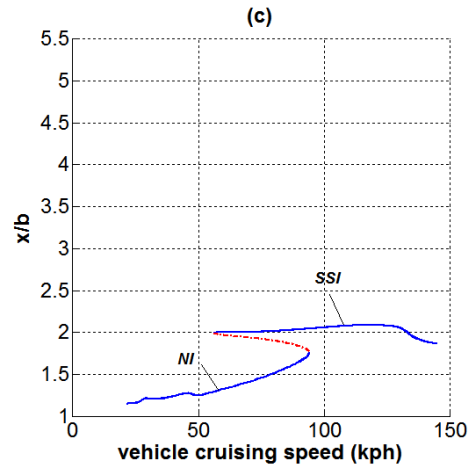
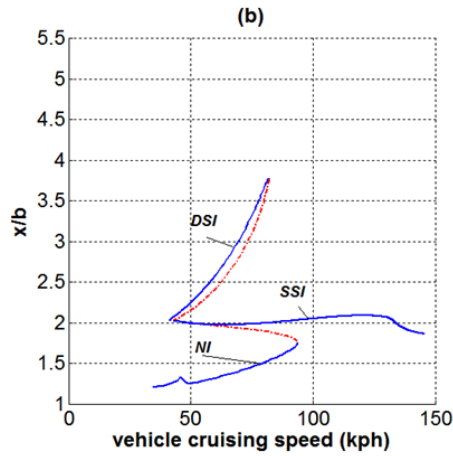
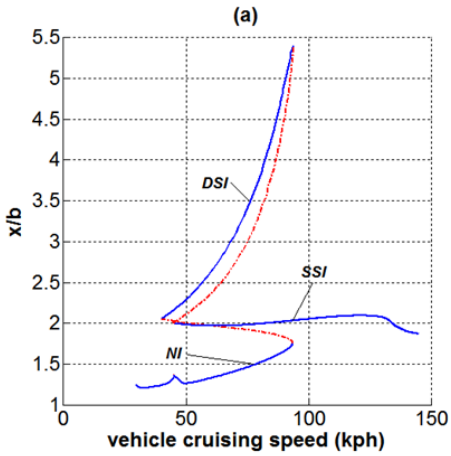
- Aerodynamic force
- +
- Rolling resistance force
- +
- Gravity force in roads with slope



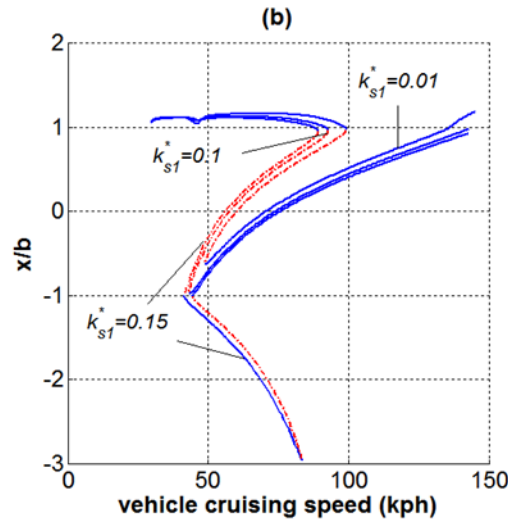
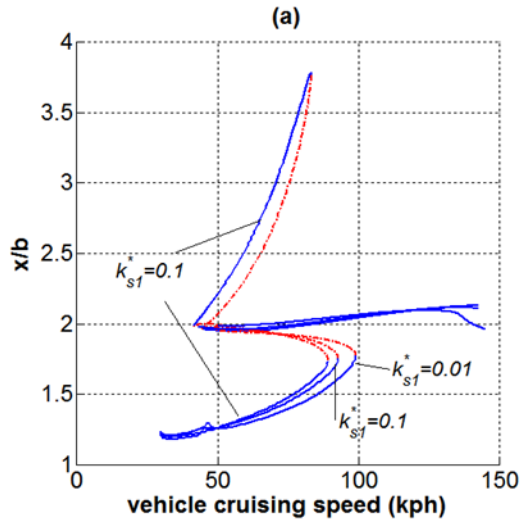
It is assumed that during cruising the engine provides the necessary power to overcome the resisting torque on wheels



# Results - Damping effect

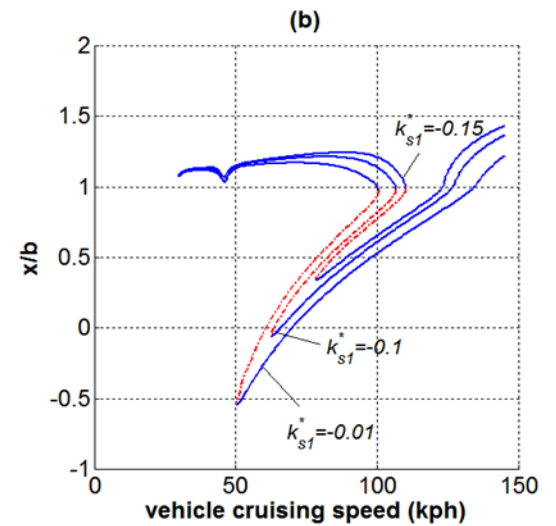
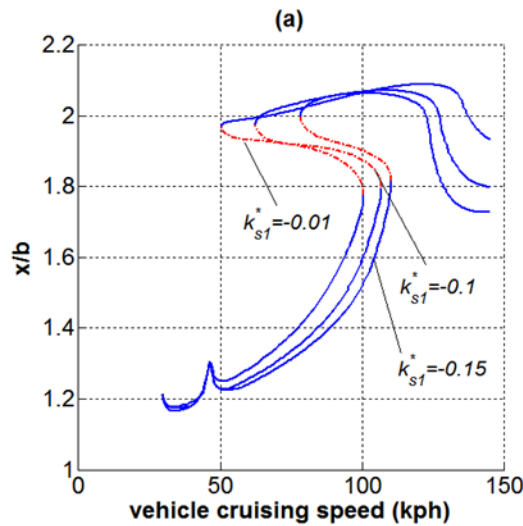


# Results - Mesh stiffness effect

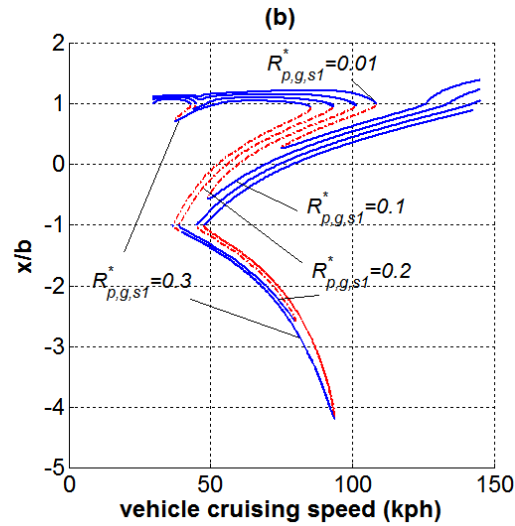
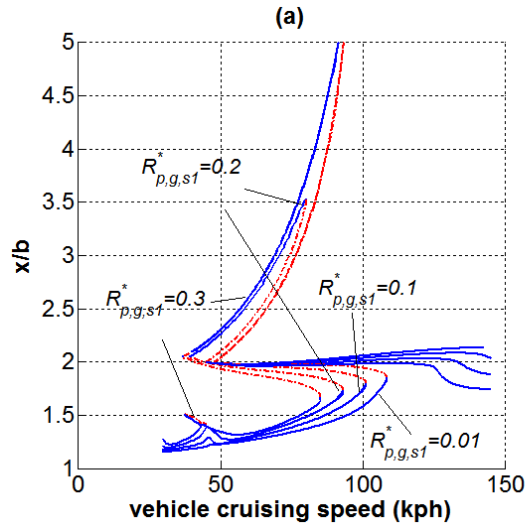


Out of phase with TE

In phase with TE

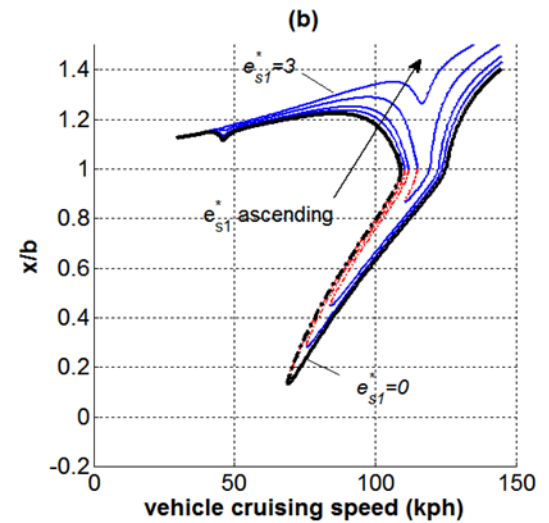
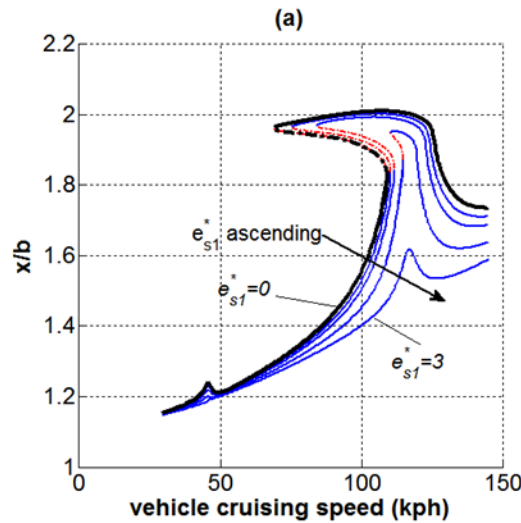


# Results - Contact radii and TE effect



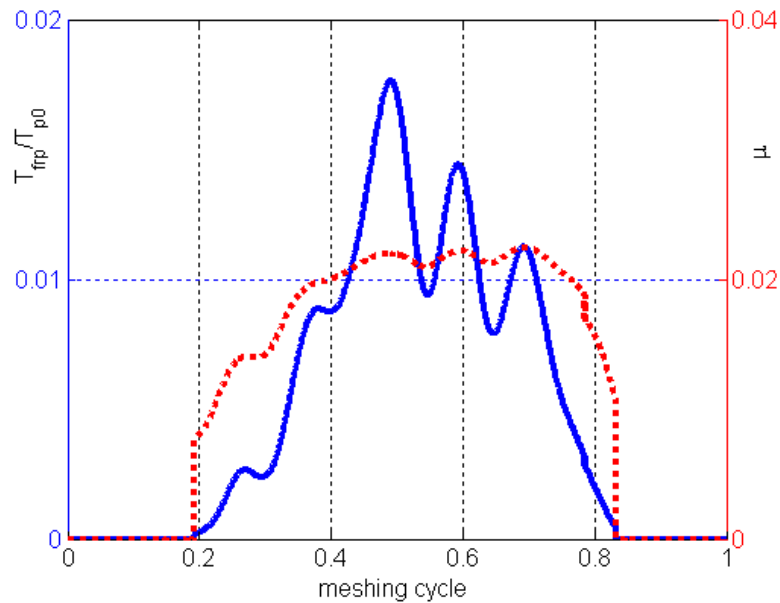
Contact radii in phase with the mesh stiffness and out of phase with the TE

Contact radii in phase with the TE

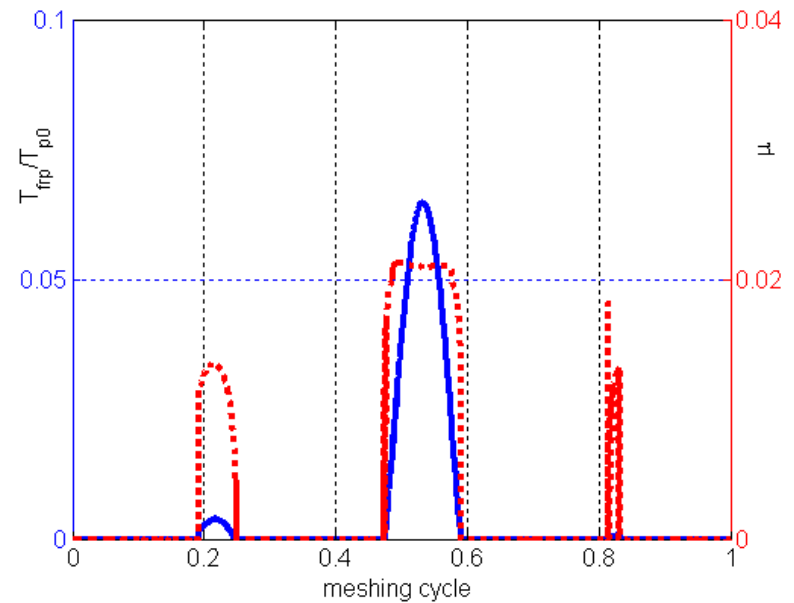


# Results - Friction coefficient and corresponding Torque

Pinion speed 1800 RPM  
(continuous contact)

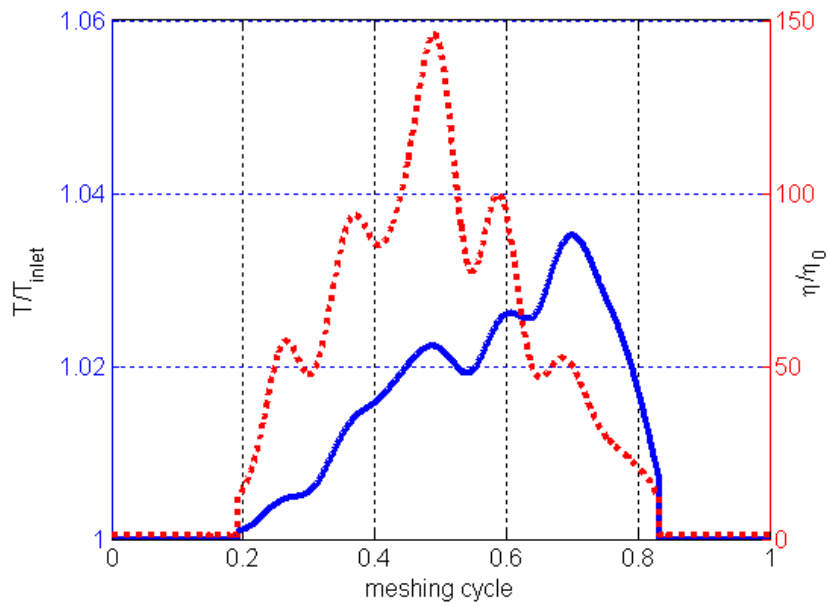


Pinion speed 3600 RPM  
(loss of contact)

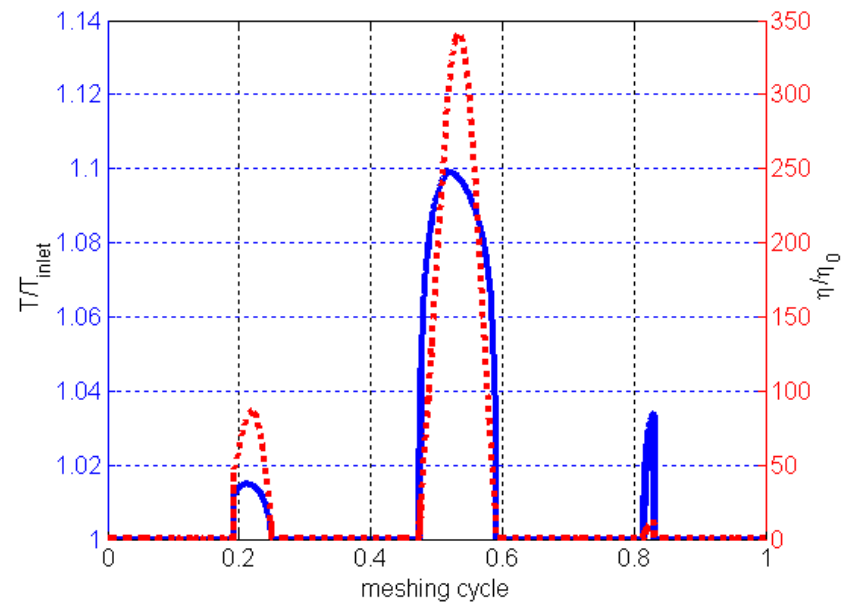


# Results - Lubricant Temperature and viscosity variation

**Pinion speed 1800 RPM  
(continuous contact)**

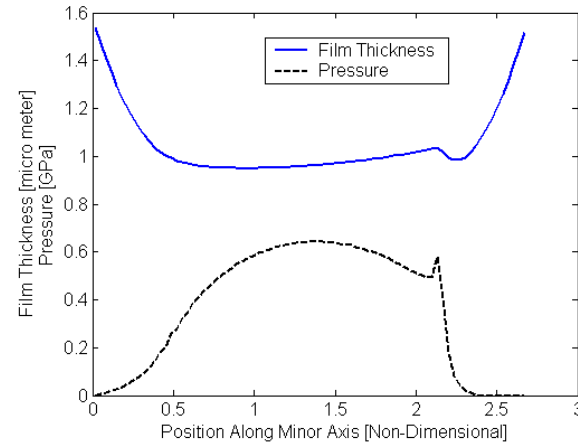
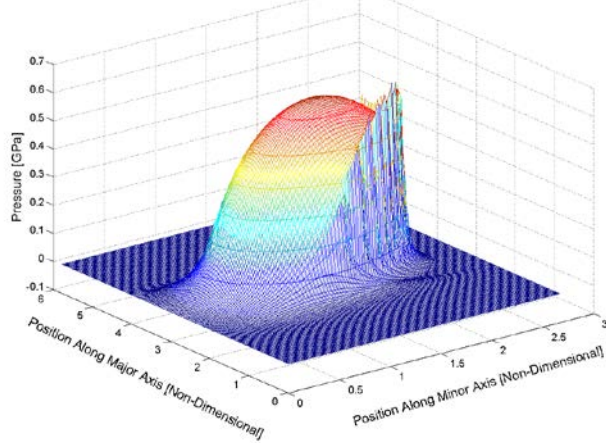


**Pinion speed 3600 RPM  
(loss of contact)**

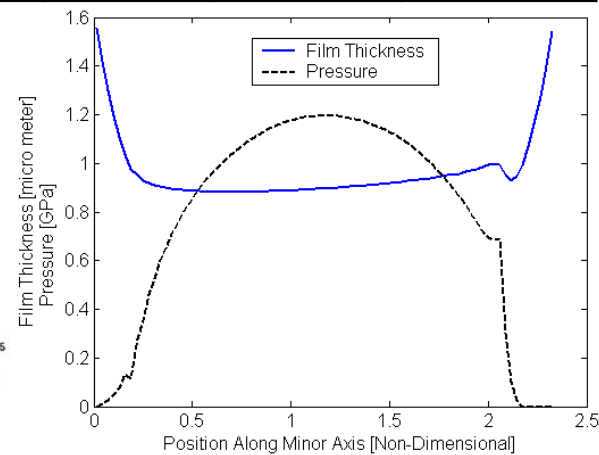
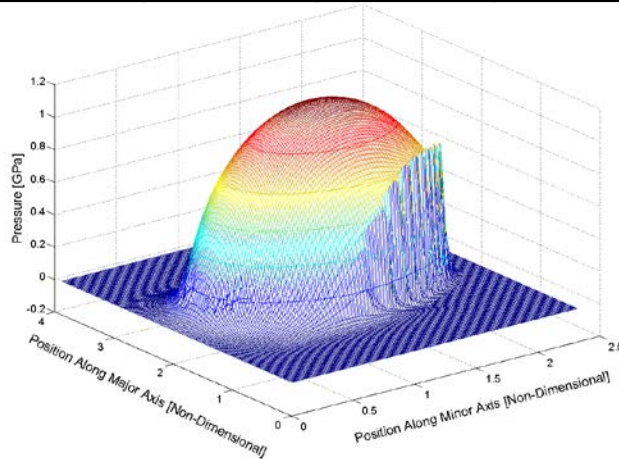


# Results - Elastohydrodynamic Lubrication

pinion angle	Load [N]	Magnitude of Velocity [m/s]	Velocity Along Minor Axis [m/s]	Velocity Along Major Axis [m/s]	Surface Radius in Minor Axis [m]	Surface Radius in Major Axis [m]
0.5027	744.5161	18.0398	7.9751	16.1813	0.0157	1.0067

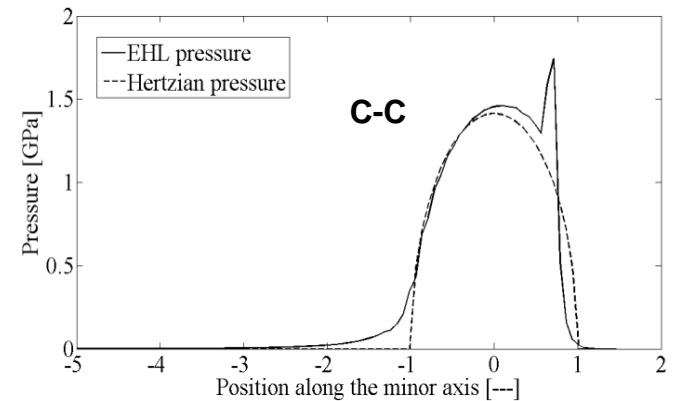
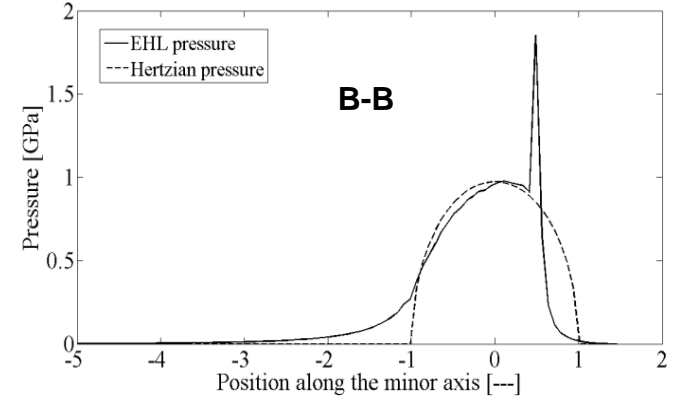
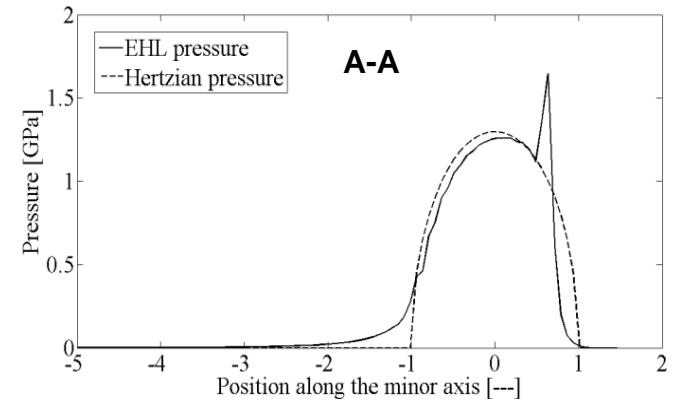
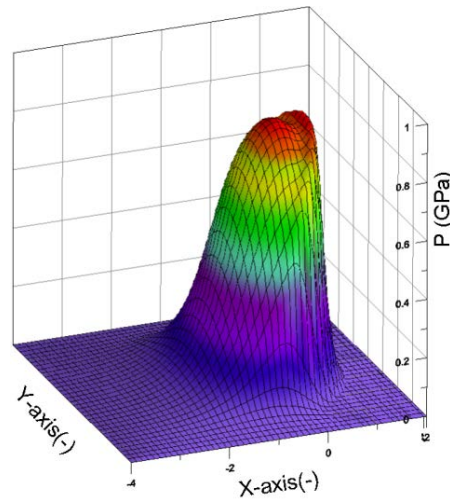
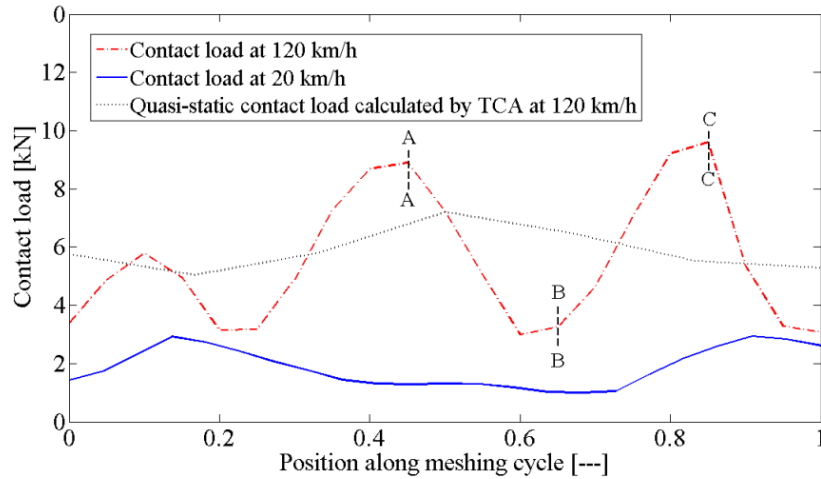


pinion angle	Load [N]	Magnitude of Velocity [m/s]	Velocity Along Minor Axis [m/s]	Velocity Along Major Axis [m/s]	Surface Radius in Minor Axis [m]	Surface Radius in Major Axis [m]
0.9582	5764.1	15.7962	8.9823	12.9938	0.0180	1.2578

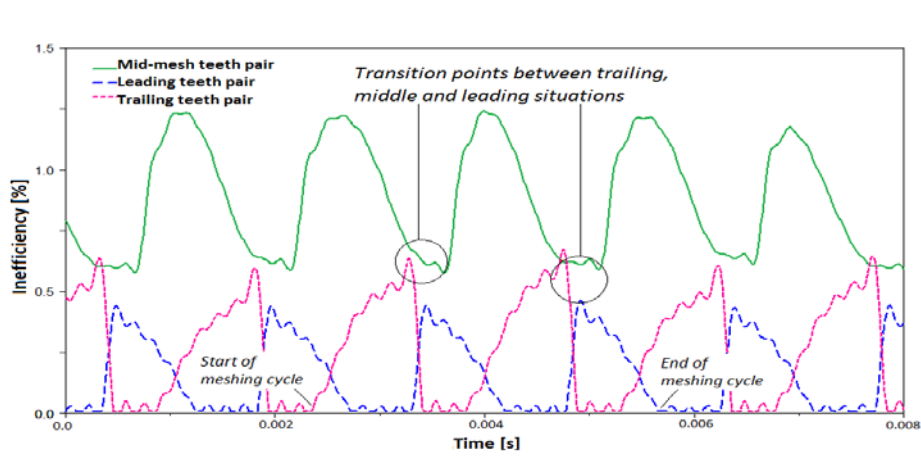




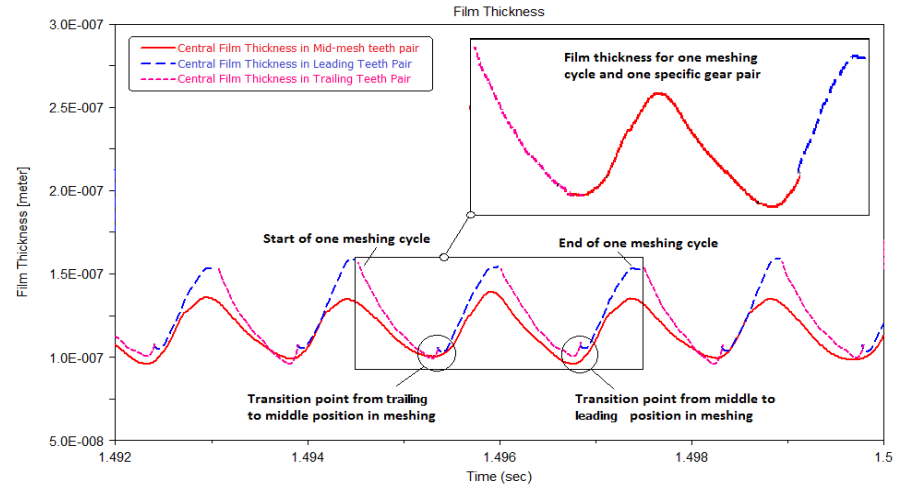
# Results - Elastohydrodynamic Lubrication



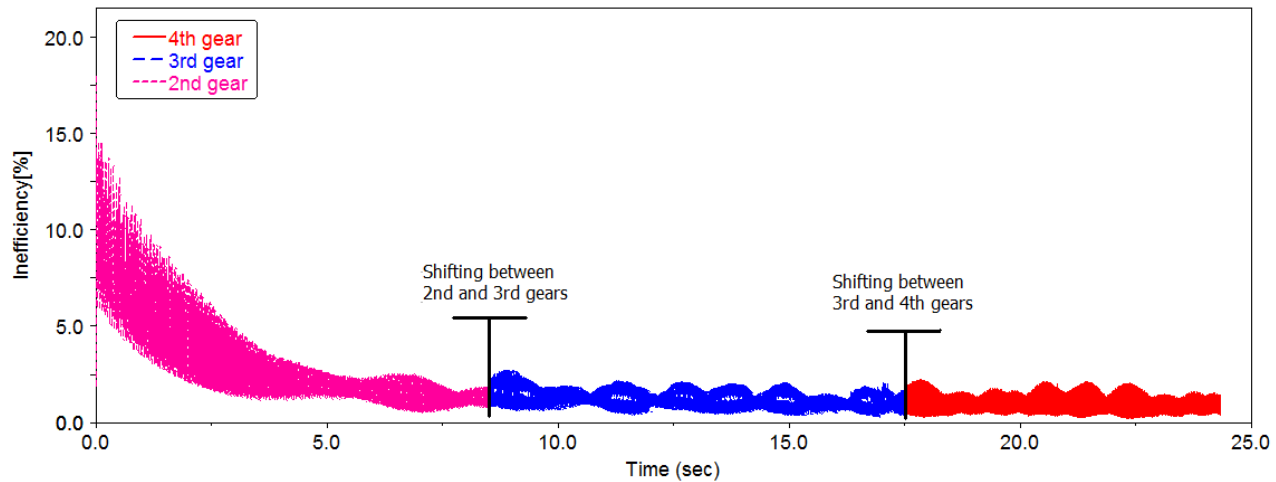
# Results - Efficiency (Viscous – Boundary Friction)



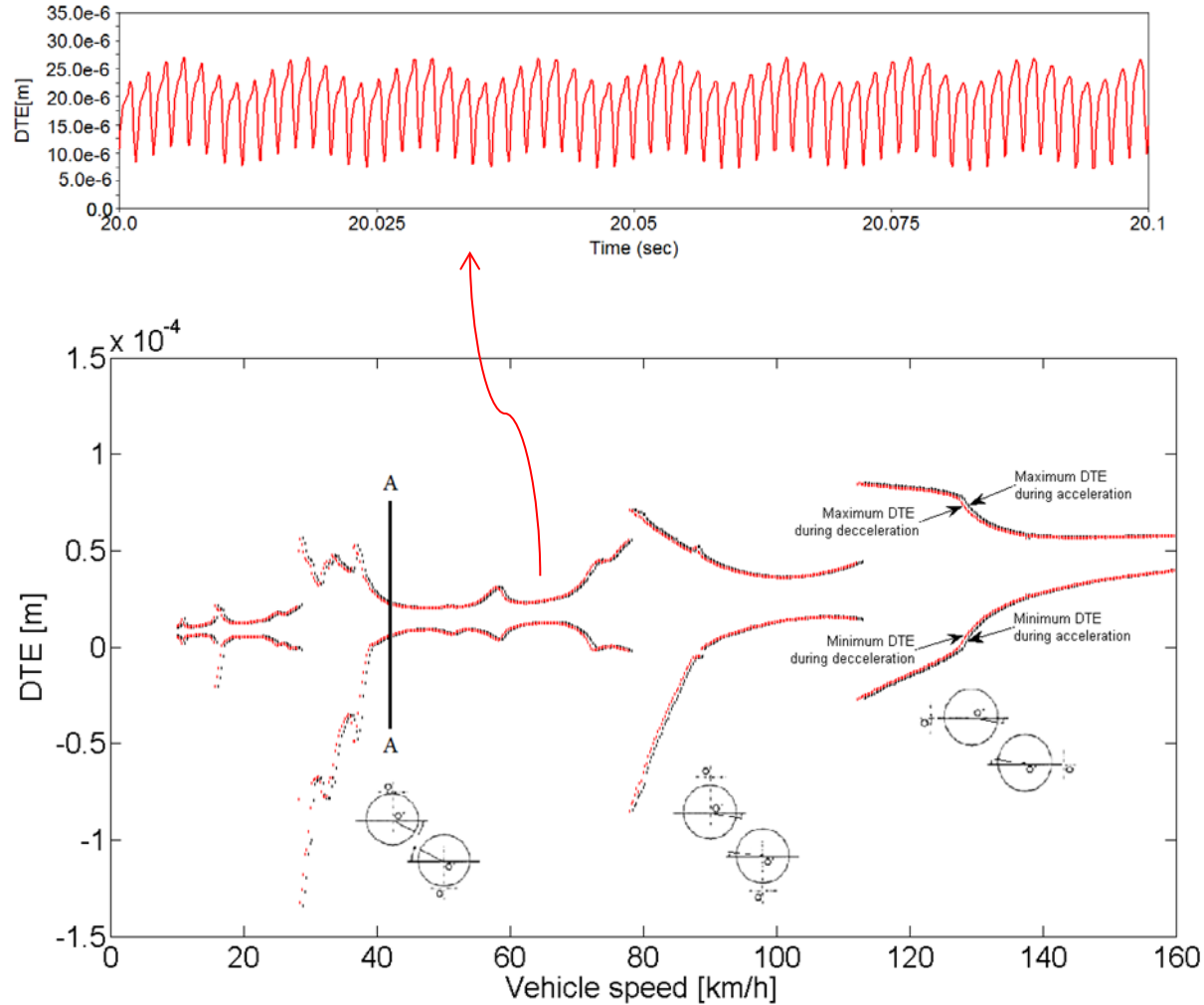
Inefficiency variation per teeth pair contact



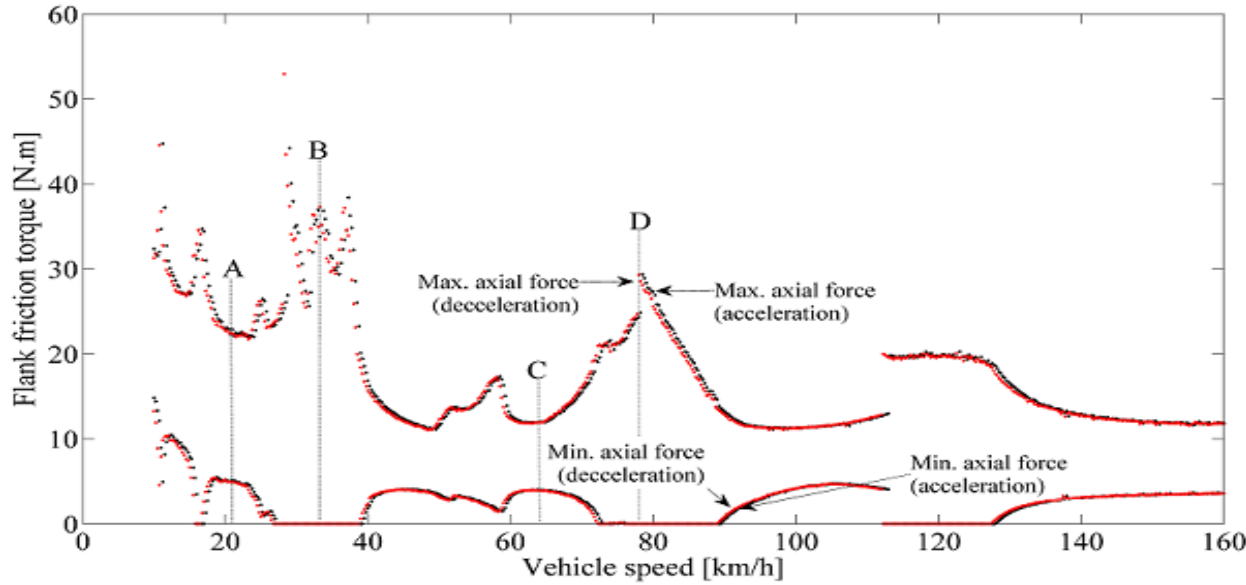
Film Thickness Time History



# Results - Dynamic Transmission Error (NVH)



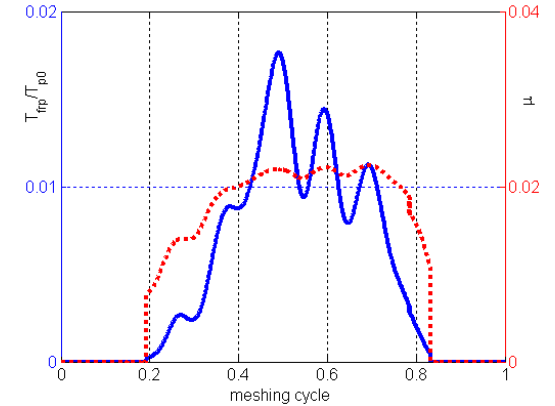
# Results - NVH versus Efficiency



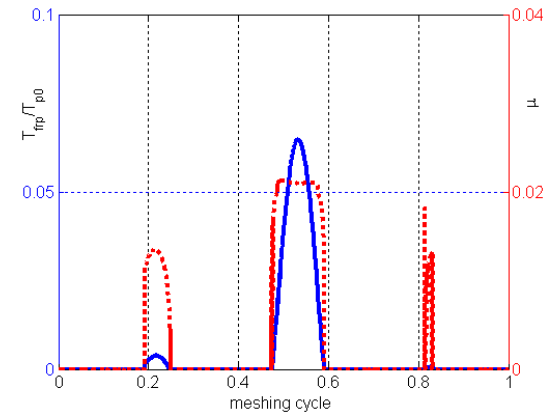
Mohammadpour et al. Multiphysics investigations on the dynamics of differential hypoid gears, *ASME Journal of Vibration and Acoustics*, 2014, DOI: 10.1115/1.4027403

Karagiannis et al. On the dynamics of lubricated hypoid gears. *Mechanism and Machine Theory*, 2012, 48, 94-120.

Continuous teeth contact (A, C)



Loss of teeth contact (B, D)



Points	A	B	C	D
Frictional energy loss during one meshing cycle (kJ)	12.75	7.37	7.15	1.58

# Conclusions

- Dynamics and Tribology are essential to study the parasitic losses (efficiency) of lubricated mechanical systems
- The two approaches need to be integrated and solved interactively due to their strong physical relationships
- The dynamics return the transient/steady state behaviour of the mechanical system, as a predictive tool for NVH severity
- Tribology / friction studies provide information about the energy efficiency of the mechanical system

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- M. Mohammadpour, S. Theodossiades and H. Rahnejat. Elastohydrodynamic lubrication of hypoid gear pairs at high loads. *Proc. of the Inst. of Mech. Eng. Part J: Journal of engineering Tribology*, 2012, 226(3), 183-198.
- I. Karagiannis, S. Theodossiades and H. Rahnejat. On the dynamics of lubricated hypoid gears. *Mech. and Mach. Theory*, 2012, 48, 94-120.
- Theodossiades, S and Karagiannis, S (2013) [An Alternative Formulation of the Dynamic Transmission Error to Study the Oscillations of Automotive Hypoid Gears](#), *Journal of Vibration and Acoustics: Transactions of the ASME*, 136
- Theodossiades, S, Mohammadpour M, Rahnejat H, Kelly P, (2013) [Transmission efficiency and noise, vibration and harshness refinement of differential hypoid gear pairs](#), *Proceedings of the Institution of Mechanical Engineers, Part K: Journal of Multi-body Dynamics*
- Mohammad pour, M, Theodossiades, S, Rahnejat, H (2014) [Transient mixed non-Newtonian thermo-elastohydrodynamics of vehicle differential hypoid gears with starved partial counter-flow inlet boundary](#), *Proceedings of the Institution of Mechanical Engineers, Part J: Journal of Engineering Tribology*, 0(0), pp.1-15
- Mohammadpour, M, Theodossiades, S, Rahnejat, H, Saunders, T (2014) [Non-Newtonian mixed elastohydrodynamics of differential hypoid gears at high loads](#), *Meccanica*, 49(5), pp.1115-1138
- Mohammad pour, M, Theodossiades, S, Rahnejat, H [Multi-physics investigations on the dynamics of differential hypoid gears](#), *Journal of Vibration and Acoustics*
- Lubrication analysis and sub-surface stress field of an automotive differential hypoid gear pair under dynamic loading, Paouris L., Theodossiades S., De la Cruz M., Rahnejat H., Kidson A., Hunt G., Barton W., IMechE Journal of Mechanical Engineering Science, 2015.
- Mohammad Pour, M, Johns-Rahnejat, PM, Theodossiades, S, Rahnejat, H (2015) [Effect of Tapered Roller Bearing Supports on the Dynamic Behaviour of Hypoid Gear Pair Differentials](#), *Proceedings of the Institution of Mechanical Engineers, Part D: Journal of Automobile Engineering*
- An Analytical Approach for the Prediction of Elastohydrodynamic Friction with Inlet Shear Heating and Starvation, Paouris, L., Rahmani, R., Theodossiades, S., Rahnejat, H., Hunt, G., Barton, W., *Tribology Letters*, 2016.



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**Thank you!**